



On October 9, 2009 the LCROSS spacecraft and its companion Centaur upper stage, impacted the lunar surface within the shadowed crater Cabeus located near the moon's South Pole. The Centaur impact speed was 9,000 km/hr with a mass of 2.2 tons.

The impact created a crater about 20 meters across and about 3 meters deep. Some of the excavated material formed a plume of debris visible to the LCROSS satellite as it flew by. Instruments on LCROSS detected about 25 gallons of water.

Problem 1 - The volume of the crater can be approximated as a cylinder with a diameter of 20 meters and a height of 3 meters. From the formula $V = \pi R^2 h$, what was the volume of the lunar surface excavated by the LCROSS-Centaur impact in cubic meters?

Problem 2 - If the density of the lunar soil (regolith) is about 3000 kilograms/meter³, how many tons of regolith were excavated by the impact?

Problem 3 - During an impact, most of the excavated material remains as a ring-shaped ejecta blanket around the crater. For the LCROSS crater, the ejecta appeared to be scattered over an area about 70 meters in diameter and perhaps 0.2 meter thick around the crater. How many tons of regolith from the crater remained near the crater?

Problem 4 - If the detected water came from the regolith ejected in the plume, and not scattered in the ejecta blanket, what was the concentration of water in the plume in units of tons of regolith per liter of water?

Problem 1 - The volume of the crater can be approximated as a cylinder with a diameter of 20 meters and a height of 3 meters. From the formula $V = \pi R^2 h$, what was the volume of the lunar surface excavated by the LCROSS-Centaur impact in cubic meters?

Answer: $V = (3.14) \times (10 \text{ meters})^2 \times 3 = \mathbf{942 \text{ cubic meters}}$.

Problem 2 - If the density of the lunar soil (regolith) is about 3000 kilograms/meter³, how many tons of regolith were excavated by the impact?

Answer: $3000 \text{ kg/m}^3 \times (942 \text{ meters}^3) = 2,800,000 \text{ kilograms}$. Since $1000 \text{ kg} = 1 \text{ ton}$, there were **2,800 tons of regolith excavated**.

Problem 3 - During an impact, most of the excavated material remains as a ring-shaped ejecta blanket around the crater. For the LCROSS crater, the ejecta appeared to be scattered over an area about 70 meters in diameter and perhaps 0.2 meter thick around the crater. How many tons of regolith from the crater remained near the crater?

Answer: The area of the ejecta blanket is given by $A = \pi(35 \text{ meters})^2 - \pi(10 \text{ meters})^2 = 3,846 - 314 = 3500 \text{ meters}^2$. The volume is $A \times h = (3500 \text{ meters}^2) \times 0.2 \text{ meters} = 700 \text{ meters}^3$. Then the mass is just $M = (700 \text{ meters}^3) \times (3,000 \text{ kilograms/meter}^3) = 2,100,000 \text{ kilograms}$ or **2,100 tons in the ejecta blanket**.

Problem 4 - If the detected water came from the regolith ejected in the plume, and not scattered in the ejecta blanket, what was the concentration of water in the plume in units of tons of regolith per liter of water?

Answer: The amount of ejected regolith was 2,800 tons - 2,100 tons or 700 tons. The detected water amounted to 25 gallons or $25 \text{ gallons} \times (3.78 \text{ liters}/1 \text{ gallon}) = 95 \text{ liters}$. So the concentration was about $C = 700 \text{ tons}/95 \text{ liters} = \mathbf{7 \text{ tons/liter}}$.

Note to teacher: The estimated concentration, C, in Problem 4 is based on an approximated geometry for the crater (cylinder), an average thickness for the ejecta blanket (about 0.2 meters) and whether all of the remaining material (700 tons) was actually involved in the plume measured by LCROSS. Students may select, by scaled drawing, other geometries for the crater, and thickness for the ejecta blanket to obtain other estimates for the concentration, C. The scientific analysis of the LCROSS data may eventually lead to better estimates for C.