



Recent Hubble Space Telescope studies of Pluto have confirmed that its atmosphere is undergoing considerable change, despite its frigid temperatures. The images, created at the very limits of Hubble's resolving power, show enigmatic light and dark regions that are probably organic compounds (dark areas) and methane or water-ice deposits (light areas). Since these photos are all that we are likely to get until NASA's New Horizons spacecraft arrives in 2015, let's see what we can learn from the image!

**Problem 1** - Using a millimeter ruler, what is the scale of the Hubble image in kilometers/millimeter?

**Problem 2** - What is the largest feature you can see on any of the three images, in kilometers, and how large is this compared to a familiar earth feature or landmark such as a state in the United States?

**Problem 3** - The satellite of Pluto, called Charon, has been used to determine the total mass of Pluto. The mass determined was about  $1.3 \times 10^{22}$  kilograms. From clues in the image, calculate the volume of Pluto and determine the average density of Pluto. How does it compare to solid-rock ( $3000 \text{ kg/m}^3$ ), water-ice ( $917 \text{ kg/m}^3$ )?

**Inquiry:** Can you create a model of Pluto that matches its average density and predicts what percentage of rock and ice may be present?

**Problem 1** - Using a millimeter ruler, what is the scale of the Hubble image in kilometers/millimeter? Answer: The Legend bar indicates 2,300 km and is 43 millimeters long so the scale is  $2300/43 = 53 \text{ km/mm}$ .

**Problem 2** - What is the largest feature you can see on any of the three images, in kilometers, and how large is this compared to a familiar earth feature or landmark such as a state in the United States?

Answer; Student's selection will vary, but on the first image to the lower right a feature measures about 8 mm in diameter which is  $8 \text{ mm} \times (53 \text{ km}/1\text{mm}) = 424 \text{ kilometers wide}$ . This is about the same size as the **state of Utah!**



**Problem 3** - The satellite of Pluto, called Charon, has been used to determine the total mass of Pluto. The mass determined was about  $1.3 \times 10^{22}$  kilograms. From clues in the image, calculate the volume of Pluto and determine the average density of Pluto. How does it compare to solid-rock ( $3000 \text{ kg/m}^3$ ), water-ice ( $917 \text{ kg/m}^3$ )? Answer: From the image, Pluto is a sphere with a diameter of 2,300 km, so its volume will be  $V = 4/3 \pi (1,250,000)^3 = 8.2 \times 10^{18} \text{ meters}^3$ . Then its density is just  $D = M/V = (1.3 \times 10^{22} \text{ kilograms}) / (8.2 \times 10^{18} \text{ meters}^3)$  so  **$D = 1,600 \text{ kg/m}^3$** . This would be about the density of **a mixture of rock and water-ice**.

**Inquiry:** Can you create a model of Pluto that matches its average density and predicts what percentage of rock and ice may be present?

Answer: We want to match the density of Pluto ( $1,600 \text{ kg/m}^3$ ) by using ice ( $917 \text{ kg/m}^3$ ) and rock ( $2300 \text{ kg/m}^3$ ). Suppose we made Pluto out of half-rock and half-ice **by mass**. The volume this would occupy would be  $V = (0.5 \times 1.3 \times 10^{22} \text{ kilograms} / 917 \text{ kg/m}^3) = 7.1 \times 10^{18} \text{ meters}^3$  for the ice, and  $V = (0.5 \times 1.3 \times 10^{22} \text{ kilograms} / 3000 \text{ kg/m}^3) = 2.2 \times 10^{18} \text{ meters}^3$  for the rock, for a total volume of  $9.3 \times 10^{18} \text{ meters}^3$  for both. This is a bit larger than the actual volume of Pluto ( $8.2 \times 10^{18} \text{ meters}^3$ ) so we have to increase the mass occupied by ice, and lower the 50% by mass occupied by the rock component. The result, from student trials and errors should yield after a few iterations **about 40% ice and 60% rock**. This can be done very quickly using an Excel spreadsheet. For advanced students, it can also be solved exactly using a bit of algebra.