The bright star Fomalhaut, in the constellation Piscis Austrinus (The Southern Fish) is only 25 light years away. It is 2000° K hotter than the Sun, and nearly 17 times as luminous, but it is also much younger: Only about 200 million years old. Astronomers have known for several decades that it has a ring of dust (asteroidal material) in orbit 133 AU from the star and about 25 AU wide. Because it is so close, it has been a favorite hunting ground in the search for planets beyond our solar system. In 2008 such a planet was at last discovered using the Hubble Space Telescope. It was the first direct photograph of a planet beyond our own solar system.

In the photo below, the dusty ring can be clearly seen, but photographs taken in 2004 and 2006 revealed the movement of one special ‘dot’ that is now known to be the star’s first detected planet. The small square on the image is magnified in the larger inset square in the lower right to show the location of the planet in more detail.

**Problem 1** – The scale of the image is 2.7 AU/millimeter. If 1.0 AU = 150 million kilometers, how far was the planet from the star in 2006?

**Problem 2** – How many kilometers had the planet moved between 2004 and 2006?

**Problem 3** – What was the average speed of the planet between 2004 and 2006 if 1 year = 8760 hours?

**Problem 4** – Assuming the orbit is circular, with the radius found from Problem 1, about how many years would it take the planet to make a full orbit around its star?

Space Math

http://spacemath.gsfc.nasa.gov
**Answer Key**

**Problem 1** – The scale of the image is 2.7 AU/millimeter. If 1.0 AU = 150 million kilometers, how far was the planet from the star in 2006?

Answer: The distance from the center of the ring (location of star in picture) to the center of the box containing the planet is 42 millimeters, then $42 \times 2.7 \text{ AU/mm} = 113 \text{ AU}$. Since 1 AU = 150 million km, the distance is $113 \times 150 \text{ million km} = 17 \text{ billion kilometers}$.

**Problem 2** – How many kilometers had the planet moved between 2004 and 2006?

Answer: On the main image, the box has a width of 4 millimeters which equals $4 \times 2.7 = 11 \text{ AU}$. The inset box showing the planet has a width of 36 mm which equals 11 AU so the scale of the small box is $11\text{AU}/36 \text{ mm} = 0.3 \text{ AU/mm}$. The planet has shifted in position about 4 mm, so this corresponds to $4 \times 0.3 = 1.2 \text{ AU or 180 million km}$.

**Problem 3** – What was the average speed of the planet between 2004 and 2006 if 1 year = 8760 hours?

Answer: The average speed is $180 \text{ million km}/17520 \text{ hours} = 10,273 \text{ km/hr}$.

**Problem 4** – Assuming the orbit is circular, with the radius found from Problem 1, about how many years would it take the planet to make a full orbit around its star?

Answer: The radius of the circle is 113 AU so the circumference is $2 \pi R = 2(3.141)(113 \text{ AU}) = 710 \text{ AU}$. The distance traveled by the planet in 2 years is, from Problem 2, about 1.2 AU, so in 2 years it traveled $1.2/710 = 0.0017$ of its full orbit. That means a full orbit will take $2.0 \text{ years}/0.0017 = 1,176 \text{ years}$.

Note - Because we are only seeing the 'projected' motion of the planet along the sky, the actual speed could be faster than the estimate in Problem 3, which would make the estimate of the orbit period a bit smaller than what students calculate in Problem 4.

*A careful study of this system by its discoverer, Dr. Paul Kalas (UC Berkeley) suggests an orbit distance of 119 AU, and an orbit period of 872 years.*