



This image was taken by the Deep Impact spacecraft on September 20 as it approaches Comet Hartley 2 from a distance of 46 million kilometers.

On November 4, the spacecraft will approach to within 700 kilometers of the surface of the comet.

The image area is 0.29 degrees on a side, and the nucleus of the comet is about 1 kilometer in diameter. The comet can be seen as the fuzzy spot near the center.

Whenever you look at a distant object, you see the object's angular size not its actual physical size. There is a simple formula that relates the actual size and distance to an object, to its apparent angular size:

$$\tan\left(\frac{\theta}{2}\right) = \frac{d}{2R}$$

where d is the object's width or diameter in kilometers, and R is its distance from the observer in kilometers. For example, a DVD disk ($d=12$ cm) held at arms-length ($R=24$ cm) will subtend an angle of $\theta = 28$ degrees.

Problem 1 - Deep Impact will pass to within 700 km of the nucleus. How big will the comet nucleus appear to the Deep Impact spacecraft if its diameter is 1 kilometer?

Problem 2 - The Deep Impact High-Resolution Imager (HRI) has a format of 1024 x 1024 pixels and a field of view of 0.118 degrees. A single pixel sees an angular field of $0.118 \text{ deg}/1024 \text{ pix} = 0.000115$ degrees. At a distance of 700 km, what linear distance will a pixel resolution of 0.000115 degrees represent?

Problem 3 - How many pixels across will the comet nucleus appear in the image taken at closest approach with the HRI?

Problem 1 - Deep Impact will pass to within 700 km of the nucleus. How big will the comet nucleus appear to the Deep Impact spacecraft if its diameter is 1 kilometer?

Answer: $d = 1$ kilometer, and $R = 700$ km, so solving for θ in the formula we have

$$\tan(\theta/2) = \frac{d}{2R} \quad \text{so } \tan(\theta/2) = 1 \text{ kilometer} / (2 \times 700), \text{ and so } \theta = \mathbf{0.08 \text{ degrees}}$$

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Answer: $\tan(0.000115) = L/700 \text{ km}$ so
 $L = 700 \tan(0.000115) \text{ km}$ **$L = 1.4 \text{ meters/pixel}$** .

Problem 3 - How many pixels across will the comet nucleus appear in the image taken at closest approach with the HRI?

Answer: The resolution of the imager is 1.4 meters/pixel. The diameter of the nucleus is believed to be about the 1 kilometer, so the comet nucleus will subtend about $1,000 \text{ meters} \times (1 \text{ pixel}/1.4 \text{ meters}) = \mathbf{714 \text{ pixels}}$. Below is an image taken by the Lunar Reconnaissance Orbiter at a resolution of 1 meter showing the Apollo 11 landing area on the moon. A similar-resolution image will be possible for Comet Hartley 2 using HRII

