



The most advanced theories of how gravity works have proposed that empty space is not smooth, but may be filled by invisible lumps and bumps that distort space into a froth of bubbles that are billions of times smaller than atomic nuclei. That's why we have not detected them in laboratory experiments thus far.

By studying how intense gamma-rays travel through the vast spaces between galaxies in the universe, NASA's Fermi Gamma-ray Observatory may have placed limits on this frothiness that eliminate many of the theories being explored to date.

As the gamma-rays travel through space, the shortest-wavelength gamma-rays take a slightly different path through space than the longer-wavelength gamma-rays. Although all gamma-rays travel at the speed of light, the invisible lumps in space scatter the short-wavelength (high-energy) gamma rays more than the long-wavelength (low-energy) ones so that there is a difference in the travel times of the long and short-wavelength gamma rays. This means that in traveling a distance, L , to Earth, the time should be about $t = L/c$ where c is the speed of light. The theories predict that the lumps in space cause the arrival times for the long and short-wavelength gamma-rays to differ by an amount $T = (L/c) \times (d/\lambda)$. In this equation, λ is the wavelength difference between the two gamma-rays (related to their energy-difference), d is the length scale corresponding to the lumpiness in space, and c is the speed of light, 3×10^{10} cm/sec.

Problem 1 – Suppose two rays of visible light differed in wavelength by 100 nanometers ($\lambda = 10^{-9}$ cm) and traveled from the sun to Earth ($L=150$ million kilometers) through space with a lumpiness of about the scale of an atomic nucleus ($d=10^{-14}$ cm). What would be the arrival time delay in seconds at Earth between the two visible light photons?

Problem 2 – Suppose there is no indication that arriving visible light photons (10^{-9} cm) experience any delays in arrival time longer than 1 second, from quasars as far away as 5 billion light years. What is the maximum size of the lumps in space that are consistent with this limit?

Problem 3 – The Fermi Telescope measured a gamma-ray pulse from a distant object located 10 billion light years from Earth. The time delay was no more than 0.7 seconds. The wavelength difference in the gamma-rays was 4.0×10^{-12} centimeters (33 billion electron volts of energy). What is the largest size that can be involved in the lumpiness of empty space given this Fermi measurement.

Problem 1 – Suppose two rays of visible light differed by 100 nanometers (10^{-9} cm) in wavelength, and traveled from the sun to earth (150 million kilometers) through space with a lumpiness of about the scale of an atomic nucleus (10^{-14} cm). What would be the arrival time delay in seconds at Earth between the two visible light photons?

Answer: $T = (1.5 \times 10^{13} \text{ cm}) \times (1.0 \times 10^{-14}) / (3 \times 10^{10} \times 1.0 \times 10^{-9})$
= 0.005 seconds.

Problem 2 – Suppose there is no indication that arriving visible light photons (10^{-9} cm) experience any delays in arrival longer than one second, from quasars as far away as 5 billion light years. What is the maximum size of the lumps in space that are consistent with this limit?

Answer: $L = 5$ billion light years; $\lambda = 10^{-9}$ cm ; $T = 1$ second
 Also $L/c = 5$ billion light years/c
 = 5 billion years.
 = 5×10^9 years $\times 3.1 \times 10^7$ sec/year
 = 1.6×10^{17} seconds

So $d = T \lambda c / L$
 = $(1 \text{ sec}) \times (1.0 \times 10^{-9} \text{ cm}) / (1.6 \times 10^{17} \text{ sec})$
 = **6.3×10^{-27} centimeters.**

Note: This is 10 trillion times smaller than the size of an atomic nucleus!

Problem 3 – The Fermi Telescope measured a gamma-ray pulse from a distant object located 10 billion light years from Earth. The time delay was no more than 0.7 seconds. The wavelength difference in the gamma-rays was 4.0×10^{-12} centimeters. What is the largest size that can be involved in the lumpiness of empty space given this Fermi measurement.

Answer: $L = 10$ billion light years; $\lambda = 4.0 \times 10^{-12}$ cm ; $T = 0.7$ second
 Also $L/c = 10$ billion light years/c
 = 10 billion years.
 = 1.0×10^{10} years $\times 3.1 \times 10^7$ sec/year
 = 3.1×10^{17} seconds

So $d = T \lambda c / L$
 = $(0.7 \text{ sec}) \times (4.0 \times 10^{-12} \text{ cm}) / (3.1 \times 10^{17} \text{ sec})$
 = **2.2×10^{-30} centimeters.**

Note: This is 22,000 trillion times smaller than the size of an atomic nucleus! According to some theories of the structure of space, the fundamental limit is about 1.6×10^{-33} centimeters and is called the Planck Length. The Fermi limit corresponds to about 1,400 Planck Lengths or smaller.