



Problem 1 – The volume of a cone is given by $V = 1/3\pi R^2 h$. If the base of the rocket nozzle has a radius of $r = 1.53$ meters (5-feet) and a height of $h = 4.37$ meters (13-foot), what is the approximate total volume of the J-2X rocket nozzle to the nearest 0.1 cubic meters? (Use $\pi = 3.14$)

Problem 2 – A better approximation to the shape of the curved nozzle is to break the volume up into a conical top section ($h=2.18$ meters) and a cylindrical bottom section ($h=2.18$ meters). If the base of the cone in the top section has a radius of 1.00 meter, and the average radius of the cylinder in the bottom section is $R=(1.00 + 1.53)/2 = 1.27$ meters, what is the total volume of the total nozzle to the nearest 0.1 cubic meters? (Use $\pi = 3.14$)

Problem 3 – The exact volume of the volume for this curved nozzle is given by the function

$$V(x) = 0.0094 x^4 - 0.141 x^3 + 1.10 x^2 + 0.14 x$$

where V is in cubic meters and x is the distance from the vertex of the cone to its base. What is the exact volume of the J-2X rocket nozzle to the nearest 0.1 cubic meters ?

Problem 1 – The volume of a cone is given by $V = 1/3\pi R^2 h$. If the base of the rocket nozzle has a radius of $r = 1.53$ meters and a height of $h = 4.37$ meters, what is the approximate total volume of the J-2X rocket nozzle to the nearest 0.1 cubic meters? (Use $\pi = 3.14$)

$$\text{Answer: } V = 1/3 (3.14) (1.53)^2 (4.37) = \mathbf{10.7 \text{ meters}^3}$$

Problem 2 – A better approximation to the shape of the curved nozzle is to break the volume up into a conical top section ($l=2.18$ meters) and a cylindrical bottom section ($L=2.18$ meters). If the base of the cone in the top section has a radius of 1.00 meter, and the average radius of the cylinder in the bottom section is $(1.00 + 1.53)/2 = 1.27$ meters, what is the total volume of the total nozzle to the nearest 0.1 cubic meters? (Use $\pi = 3.14$)

$$\begin{aligned} \text{Cone} &= 1/3 (3.14)(1.0)^2(2.18) = 2.28 \text{ meters}^3 \\ \text{Cylinder} &= 3.14 (1.27)^2 (2.18) = 11.04 \text{ meters}^3 \\ \text{Approximate total volume} &= \mathbf{13.3 \text{ meters}^3}. \end{aligned}$$

Problem 3 – The exact volume of the volume for this curved nozzle is given by the function $V(x) = 0.0094x^4 - 0.141x^3 + 1.10x^2 + 0.14x$ where V is in cubic meters and x is the distance in meters from the vertex of the cone to its base. What is the exact volume of the J-2X rocket nozzle to the nearest 0.1 cubic meters?

$$\begin{aligned} \text{Answer: } V(4.37\text{meters}) &= 0.0094(4.37)^4 - 0.141(4.37)^3 + 1.10 (4.37)^2 + 0.14(4.37) \\ &= 3.43 - 11.77 + 21.00 + 0.61 \\ &= 13.27 \\ &= \mathbf{13.3 \text{ meters}^3}. \end{aligned}$$