



An asteroid, or comet, viewed from Earth will be either bright or faint depending on many quantifiable factors. Of course the size of the body and its reflectivity make a big difference. So does its distance from the sun and earth at the time you see it. The brightness also depends on whether, from Earth, it is fully-illuminated like the full moon, or only partly-illuminated like the crescent moon.

Astronomers can put all of these variables together into one single equation which works pretty well to predict a body's brightness just about anywhere inside the solar system!

The streak in the photo above is the asteroid 1999AN10 (Courtesy Palomar Digital Sky Survey). Orbit data suggest that on August 7, 2027 it will pass within 37,000 kilometers of Earth. The formula for the brightness of the asteroid is given by:

$$R = 0.011 d 10^{-\frac{1}{5}(m)}$$

where: R is the asteroid radius in meters, d is the distance to Earth in kilometers, and m is the apparent brightness of the asteroid viewed from Earth. Note, the faintest star you can see with the naked eye is about $m = +6.5$. The photograph above shows stars as faint as $m = +20$. The asteroid is assumed to have a reflectivity similar to lunar rock.

Problem 1 - If the distance to the asteroid at the time of closest approach in 2027 will be $d = 37,000$ kilometers, what is the formula $R(m)$ for the asteroid?

Problem 2 - If the radius of the asteroid is in the domain between 200 meters and 1000 meters, what is the range of apparent brightnesses?

Problem 1 - If the distance to the asteroid at the time of closest approach in 2027 will be $d = 37,000$ kilometers, what is the formula $R(m)$ for the asteroid? Answer: Substitute the given values into the equation and simplify. The formula will give the radius of the asteroid in meters as a function of its apparent brightness (called apparent magnitude by astronomers) given by m .

$$R(m) = 0.011 (37000)10^{-0.2m}$$

$$R(m) = 407 10^{-0.2m}$$

Problem 2 - If the radius of the asteroid is in the domain between 200 meters and 1000 meters, what is the range of apparent brightnesses? Answer: Solve the formula for $R(m)$ for $m(R)$ and evaluate for $R = 200$ meters and $R = 1000$ meters to obtain the range of the function.

$$m(R) = -5 \log_{10}(R/4224)$$

$$\begin{array}{ll} \text{so } m(R) \text{ for } R = 200 \text{ yields } m(200) = -5 (-11.3) & \text{so } m(200) = +1.5 \\ \text{and } m(1000) = -5(0.39) & \text{so } m(1000) = -2.0 \end{array}$$

so Domain R : [200,1000]
and Range m : [+1.5, -2.0]

Note: The planet Venus can be as bright as $m = -2.5$ so this asteroid should be easily visible if it is in this size domain.