

Space Math - I

This collection of activities is based on a weekly series of space science problems distributed to thousands of teachers during 2004-2005 school year. They were intended as extra-credit problems for students looking for additional challenges in the math and physical science curriculum in grades 7 through 9. The problems were designed to be authentic glimpses of modern engineering issues that come up in designing satellites to work in space, and to provide insight into the basic phenomena of the Sun-Earth system, specifically 'Space Weather'. The problems were designed to be 'one-pagers' with the student work sheet (with the top line for the student's name) and a Teacher's Guide and Answer Key as a second page. This compact form was deemed very popular by participating teachers.

This booklet was created by the NASA, IMAGE satellite program's Education and Public Outreach Project (POETRY).

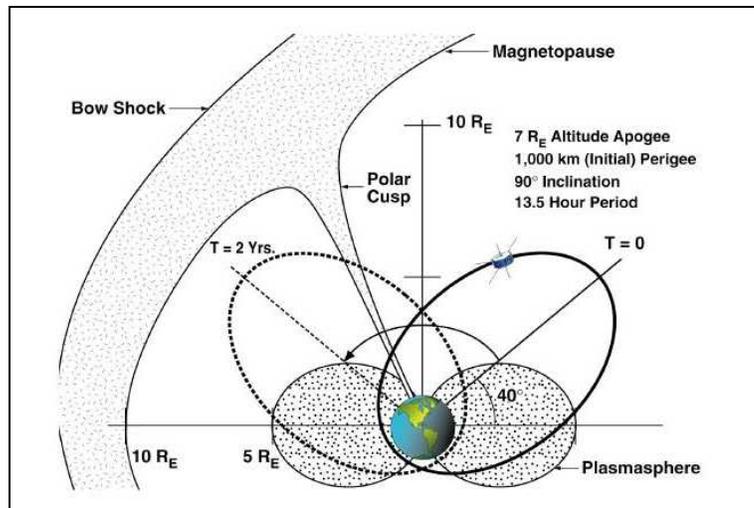
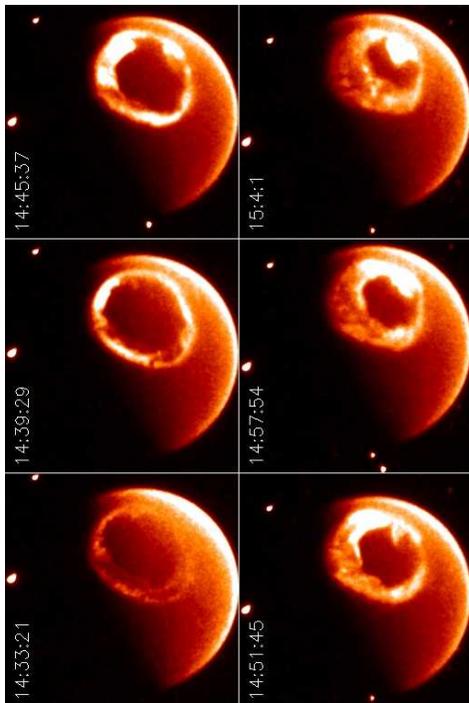
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A series of images (left) of the Northern Lights from space taken by the IMAGE satellite. The satellite orbits Earth in an elliptical path (above), which takes it into many different regions of Earth's environment in space.

For more weekly classroom activities about the Sun-Earth system visit the IMAGE website,
<http://image.gsfc.nasa.gov/poetry/weekly/weekly.html>
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Background



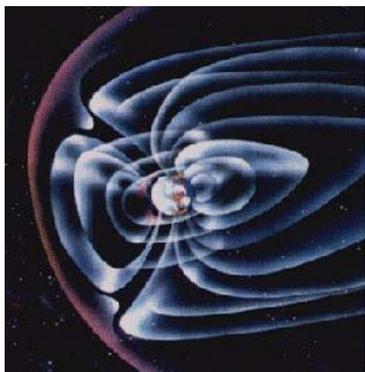
We live next to a very stormy star, the Sun, but you would hardly notice anything unusual most of the time. Its constant sunshine hides spectacular changes. Only the dazzling glow of the Northern Lights suggests that invisible forces are clashing in space. These forces may cause all kinds of problems for us, and our expensive technology. It doesn't take long for 'solar storms' to get here, either. X-rays from flares make the trip to Earth in just under 9 minutes, while the fastest moving plasma can make the journey in only 17 hours. Solar flares disrupt Earth's ionosphere and can cause satellite malfunctions, while the plasma clouds can change Earth's magnetic field. This leads to the displays of the aurora that humans have marveled at for thousands of years. Aurora light up the sky with billions of watts of power and cover millions of square kilometers. Why does all this happen? (Photo- Auroral curtain by Jan Curtis)

Space Weather



It has to do with Earth's magnetic field and how it is disturbed by solar storms and the solar wind. The wind carries its own magnetic field with it, and travels at speeds of millions of kilometers per hour. Scientists keep track of this interplanetary storminess using numbers that follow its ups and downs just like meteorologists follow a storm's speed, pressure and humidity. Periods of increased and decreased solar activity come and go every 11 years. Solar flares also have their own story to tell just like flashes of lightning in a bad storm. (Photo - Coronal Mass Ejection seen by SOHO satellite)

Models and Forecasting



Scientists have to keep track of many different kinds of phenomena in the universe, both big and small. That's why they have invented a way to write very big and very small numbers using 'scientific notation'. They also have to master how to think in three-dimensions and how to use mathematical models. Once they find the right models, they can use them to make better predictions of when the next solar storm will arrive here at Earth, and what it will do when it gets here! (Sketch of Earth's magnetic field)

On August 28, 1859 a massive solar storm caused spectacular aurora seen all over the globe. It was reported in all the major newspapers; poems were written about it; and famous artists painted its shapes and forms. It also caused severe problems with telegraph networks at the time, which lasted for many hours worldwide. Although scientists gave detailed reports of the changing forms of this vivid display, many ordinary citizens offered their own impressions of this event too. Below are two of these descriptions seen from two different locations.

Galveston, Texas:

August 28 as early as twilight closed, the northern sky was reddish, and at times lighter than other portions of the heavens. At 7:30 PM a few streamers showed themselves. Soon the whole sky from Ursa Major to the zodiac in the east was occupied by the streams or spiral columns that rose from the horizon. Spread over the same extent was an exquisite roseate tint which faded and returned. Stately columns of light reaching up about 45 degrees above the horizon moved westward. There were frequent flashes of lightning along the whole extent of the aurora. At 9:00 PM the whole of the streaking had faded leaving only a sort of twilight over the northern sky.”

London, England:

“At 0:15 AM on August 28th the auroral light in the north assumed the form of a luminous arch, similar to daybreak, and in the southwest there was an intense glare of red covering a very large extent of the sky. At 00:20 AM streamers appeared; at 00:25 AM the streamers rose to the zenith and were tinged with crimson at their summits. At 00:45 AM frequent coruscations appeared in the aurora. At 01:20 AM the arch which had partially faded began to reform and the body of the light was very strong but not bright enough to read newspaper print. At 1:30 AM the light had begun to fade. By 2:00 AM the aurora was very indistinct.”

A common problem scientists face when organizing observations from different places around the world is that observers like to note when things happened by their local time. Scientists simplify these accounts by converting them into Universal Time, which is the local time in Greenwich, England, also called Greenwich Mean Time (GMT). To make time calculations easier, UT is expressed in the 24-hour clock format so that 11:00 AM is written as 11:00, but times after noon are written, for example, as 1:00 PM is written as 13:00, and 10:00 PM is written as 22:00. Since London is very close to Greenwich, the times mentioned in the London account above are already in Universal Time and only need to be converted to the 24-hour format. For Galveston, Texas, its time is 5 hours behind UT so that to get the equivalent UT for Galveston, first convert the Galveston times to the 24-hour format, then add 5 hours.

Question 1 - From these two descriptions, can you extract the specific points of each narrative? What are their similarities?

Question 2 - From the sequences of events in each description, can you create a timeline for the aurora display that fits the most details?

Question 3 - Why was the aurora observed to reach closer to zenith in London than in Galveston?

Question 1 - From these two descriptions, can you extract the specific points of each narrative? What are their similarities? **Answer:** Here are the main points in each story with the similarities highlighted.

Story 1:

1. Display began at end of twilight with faint **reddish light in north**.
2. 7:30 PM (00:00 UT) **streamers began to appear**
3. Streamers of spiral columns filled eastern sky
4. Faint rose-colored light covered same eastern sky, fading and returning
5. Columns of light reached **45 degrees to zenith**, and moved westwards
6. Frequent **flashes of light along the whole aurora**
7. 9:00 PM (02:00 UT), the **aurora faded** and left a twilight glow in north.

Story 2:

1. 00:15 AM (00:15 UT) - Luminous arch **appeared in northern** sky
2. 00:16 AM (00:16 UT) - Intense glare of red in southwest
3. 00:20 AM (00:20 UT) - **Streamers appeared**
4. 00:25 AM (00:25 UT) - Streamers **reached zenith** and were crimson at highest points
5. 00:45 AM (00:45 UT) - Frequent **coruscations appeared in aurora**
6. 01:20 AM (01:20 UT) - Arch begins to fade and reform
7. 01:30 AM (01:30 UT) - Aurora **begins to fade**.
8. 02:00 AM (02:00 UT) - Aurora very indistinct.

Similarities: Auroral light appeared in northern sky. Streamers appeared soon afterwards. The streamers expanded in the sky until they were nearly overhead from Galveston, and overhead in London. The aurora shapes showed activity in the form of flashes and movement (coruscations). Soon after this active phase, the aurora faded.

Question 2 - From the sequences of events in each description, can you create a common timeline for the aurora display that fits the most details?

Answer: Each student might group the events differently because the eyewitness accounts are not detailed enough. Because this aurora is seen in the Northern Hemisphere, it is properly called the aurora borealis. Here is one way to organize the timeline:

“The aurora borealis started with a faint wash of reddish light in the north. A brilliant arch of light formed. Five minutes later, streamers began to appear which were crimson at their highest points above the horizon. Then, coruscations (waves) began to appear in the brightening red glow of the aurora with the streamers filling the entire eastern sky. The columns of light and streamers began to move westwards, and frequent flashes of light were seen along the aurora as the luminous arch of began to fade and reform. After an hour and fifteen minutes, the aurora began to fade away, leaving behind a twilight glow that persisted for another half-hour.”

Question 3 - Why was the aurora observed to reach closer to zenith in London than in Galveston? **Answer-** Because the aurora is a polar phenomenon, and London is at a higher latitude than Galveston. That means that the aurora will be seen higher in the northern sky from London than from Galveston.

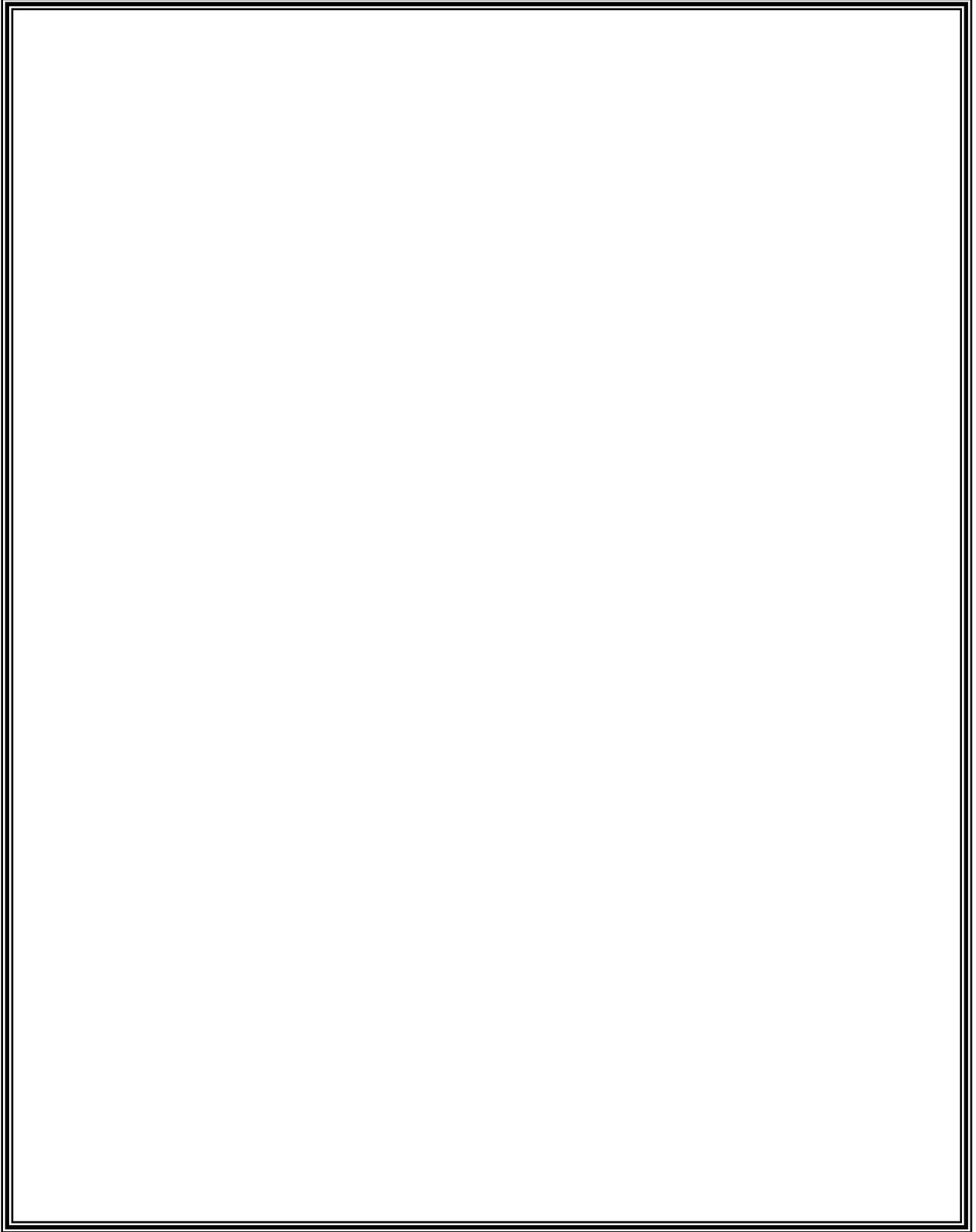
The aurora (see back page of this book) is a spectacular, visual experience for every human that has watched it. Although scientists want to study it to learn about its secrets, other observers prefer to simply experience the phenomenon for its beauty and awesome mystery. Here is a vivid description of an aurora observed on August 28, 1859 by Captain Stanard from Cleveland, Ohio.

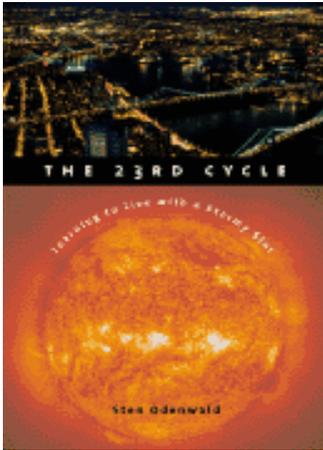
"At 9:00 PM, a belt began to rise up in the north, and as the convex edge attained a height of about 40 degrees above the horizon, it began to shoot out long, attenuated bright rays close together, moving slowly to the west and reaching to the zenith. Near the convex edge they were of a bright yellow, changing as they shot up to orange, and near the zenith to a bright red, the middle and lower ends remaining yellow and orange. As the fiery points of the rays shot into the broad belt overhead, which had still remained like a belt of luminous fog, the whole thing was changed in an instant into bright red color. The color deepening as it neared the eastern horizon, to a bright crimson, and at the western end near the star Arcturus, into a bright scarlet, gradually growing fainter in the zenith, and increasing in brightness nearer the horizon. After 15 minutes it resolved itself into converging rays that came from the zenith."

" At 9:45 PM, A double arch formed from two narrow ribbons of light 15 degrees wide running from Canes Venatici to the southern edge of Perseus. The bright star Capella shining through the narrow black space between them. Ten minutes later, bright rays suddenly shot up in quick successive flashes from the lower through the upper arch, reaching nearly to the zenith, and moving slowly to the west until they reached the constellation Corona Borealis, lighting up the northwestern sky with yellow, orange and red. There commenced a sudden flashing of horizontal wavy bands from the upper arch towards the zenith."

From the information in this description, try to recreate what Mr. Stanard saw for one particular moment as he watched the aurora dance across the sky. Use colored pencils, crayons, watercolors or other media to render a view of the aurora based on this description.

Use the following space for your rendering:





In 1999, Dr. Sten Odenwald wrote a book called ‘The 23rd Cycle: Learning to live with a stormy star’ that described all of the ways that severe space weather events, called solar storms, can affect our satellite technology, our electrical power, and even the health of astronauts and airline passengers and crew.

Read the excerpt from his book, and answer the following questions based on the information in the excerpt.

Question 1: What topic is this part of the book describing?

Question 2: Describe how a solar storm is involved with this topic?

Question 3: What does the article identify as a possible risk for passengers?

Here is a short list of your radiation exposure at ground level each year, in terms of a unit of radiation dosage called the milliRem.

| | |
|--|------------------------|
| Radon gas in your basement | 160 milliRems per year |
| The ground under your feet..... | 60 |
| Nuclear reprocessing plants..... | 40 |
| Cosmic rays at sea level..... | 38 |
| Cosmic rays from high altitude city (Denver).... | 130 |
| Medical imaging..... | 30 |
| Food and water..... | 25 |

Question 4: If you add up the different exposures in the list above, what is your total dosage each year if you were living at sea level? Living at high altitudes in Denver?

Question 5: According to the information in the article, how much extra radiation exposure would a passenger receive in a 10-hour flight at 35,000 feet?

Question 6: How much extra radiation will an airline crew member receive during 900 hours per year of flying?

Question 7: Do you think the radiation risk from solar storms is a significant one? Present the evidence that demonstrates the size of the health risk, and the evidence that suggests that the health risk is minimal.

Airline Travel and Solar Storms

Jet airliners fly at altitudes above 35,000 feet which is certainly not enough to get them into space, but it is more than enough to subject the pilots and stewardesses to some respectable doses when looked at over the course of their careers, and thousands of flights. A trip on a jet plane is often taken in a party-like atmosphere with passengers confident that, barring any unexpected accidents and food problems, they will return to Earth safely and with no lasting physical affects. But depending on what the Sun is doing, a solar storm can produce enough radiation to equal a significant fraction of a chest X-ray's dosage even at typical passenger altitudes of 35,000 feet. Airline pilots and flight attendants can spend over 900 hours in the air every year, which makes them a very big target for cosmic rays and anything else our Sun feels like adding to this mix. According to a report by the Department of Transportation, the highest dosages occur on international flights passing close to the poles where the Earth's magnetic field concentrates the particles responsible for the dosages.

Although the dosage you receive on a single such flight per year is very small, about one milliRem per hour, frequent fliers that amass over 100,000 miles per year would accumulate nearly 500 millirems each year. Airline crews who spend 900 hours in the air would absorb even higher doses, especially on polar routes. For this population, their lifetime cancer rate would be 23 cancers per 100 people. By comparison, the typical cancer rate for ground dwellers is about 22 cancers per 100. But the impact does not end with the airline crew. The federally recommended limit for pregnant women is 500 millirems per year. Even at these levels, about four extra cases of mental retardation would appear on average per 100,000 women stewardesses if they are exposed between weeks 8 to 15 in the gestation cycle. This is a time when few women realize they are pregnant, and when critical stages in neural system formation are taking place in the fetus.

Matthew H. Finucane, air safety and health director of the Association of Flight Attendants in Washington DC, has claimed that these exposure rates are alarming, and demands that the FAA to do something about it. One solution is to monitor the cabin radiation exposure and establish OSHA guidelines for it. If possible, he also wants to set up a system to warn crews of unusually intense bursts of cosmic radiation, or solar storm activity during a flight. Meanwhile, the European Aviation Agency is contemplating going even further. They want to issue standard dosimetry badges to all airline personnel so that their annual exposures can be rigorously monitored. This is a very provocative step to take, because it could have a rather chilling effect on airline passengers. It might also raise questions at the ticket counter that have never been dealt with before, *'Excuse me, can you give me a flight from Miami to Stockholm that will give me less than one chest X-ray extra dosage?'* How will the traveler process this new information, given our general nervousness over simple diagnostic X-rays?

Consider this: during September 29, 1989, for example, a powerful X-ray flare caused passengers on high-flying Concord airliners to receive dosages equal to two chest X-rays per hour. At the end of the flight, each passenger had silently received hundreds of additional millirems added to their regular background doses. Still, these occasional dosages the average person receives while flying, compared to the dosages we might accumulate once we land at another geographic location, are rather inconsequential over a lifetime. Compared to the quality of life that we gain in exchange for the minor radiation exposure we risk, most people will grudgingly admit the transaction is a bargain. Statisticians who work with insurance companies often think in terms of the number of days lost to your life expectancy from a variety of causes. On this scale, smoking 20 cigarettes a day costs you 2200 days; being overweight by 15% costs you 730 days; and an additional 300 millirem per year over the natural background dose (about 250 milliRem) reduces your life expectancy by 15 days. "

[Dr. Sten Odenwald, 'The 23rd Cycle' Columbia University Press, 2000]

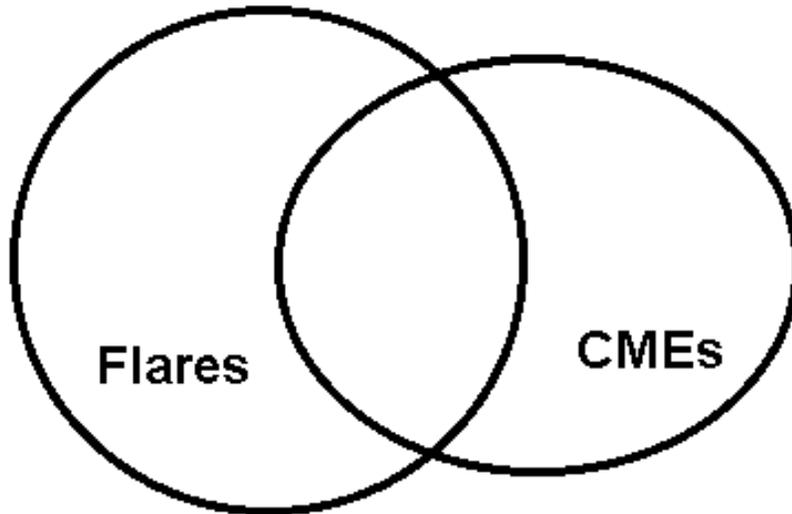
Predicting CMEs and Flares

Solar flares are violent releases of energy from the sun that last 10 to 20 minutes and produce intense flashes of x-rays. Some of these flares can cause radio interference, and problems with communication satellites. Coronal mass ejections (CMEs) are enormous releases of matter (plasma) from the sun that travel at nearly a million miles per hour to Earth. CMEs can cause the Northern Lights and sometimes result in electrical power blackouts.

During a particular month of solar activity, the following events were recorded:

| | |
|----------------------|----|
| Solar Flares | 22 |
| CME s | 12 |
| Both flares and CMEs | 7 |

A scientist decides to analyze the results to come up with an early-warning alert system. He wants to use CMEs to predict when solar flares will happen, and he wants to use flares to predict when CMEs will happen. His first step is to construct a Venn Diagram to display the data. Place the data in the correct locations.

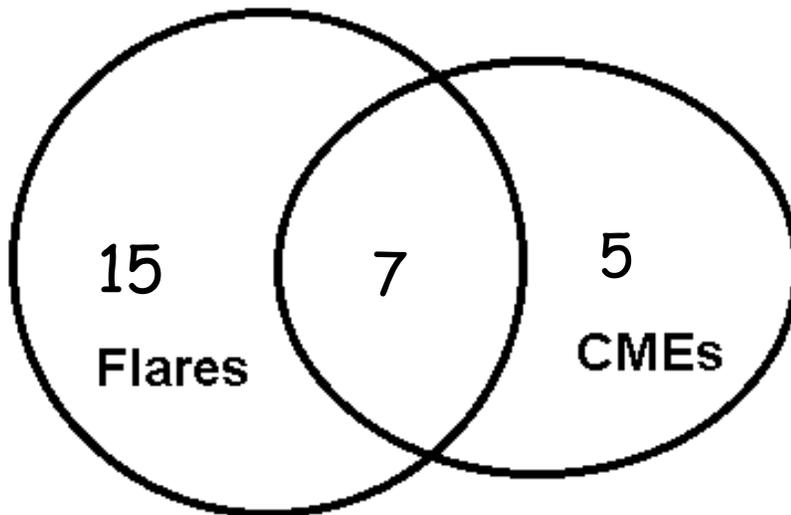


Problem 1 - What do the non-overlapping parts of the diagram represent?

Problem 2 - Based on this data, if you see a flare on the sun, what is the probability that a CME will also occur?

Problem 3 - Based on this data, if you see a CME, what is the probability that a flare will also occur?

Problem 4 - In your own words, explain which early warning system gives you the best prediction of what a particular kind of solar storm will occur.



Problem 1 - What do the non-overlapping parts of the diagram represent?

Answer: They represent solar storm events where only CMEs are seen, or only flares are seen but not both happening at the same time.

Problem 2 - Based on this data, if you see a flare on the sun, what is the probability that a CME will also occur?

Answer: The number of flares that occur at the same time as a CME is 7, so $7/12$ is the probability that if you see a flare, you will also see a CME.

Problem 3 - Based on this data, if you see a CME, what is the probability that a flare will also occur?

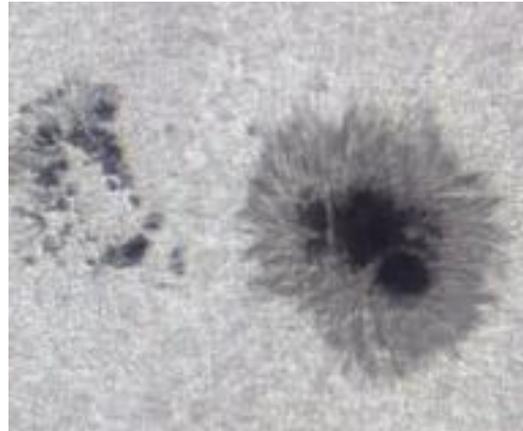
Answer: There are 22 CMEs so the probability is $7/22$ that, given you see a CME you will also see a flare.

Problem 4 - In your own words, explain which early warning system gives you the best prediction of what a particular kind of solar storm will occur.

Answer: Because $7/12$ is larger than $7/22$, an early warning system that uses flares to predict CMEs will be more reliable than a system that uses CMEs to predict flares. This means that you have a better chance of predicting when an electrical outage (caused by a CME) will occur than when a satellite problem (caused by a flare) will occur using these warning systems.

Sunspots are some of the most interesting, and longest studied, phenomena on the sun's surface. The table below shows the area of a sunspot. In comparison, the surface area of Earth is '169' units on the sunspot scale. The table also shows the brightest flare seen from the vicinity of the sunspot s beginning November 6, 2004. Flares are ranked by their brightness 'C', 'M' and 'X' with M-class flares being 10x more luminous than C-class flares, and X-class flares being 10x brighter than M-class flares.

| Date | Spot # | Area | Flare |
|--------|--------|------|-------|
| Nov 6 | #696 | 820 | M |
| Nov 7 | #696 | 910 | M |
| Nov 8 | #696 | 650 | X |
| Nov 10 | #696 | 730 | M |
| Nov 11 | #696 | 470 | X |
| Dec 2 | #708 | 130 | M |
| Dec 3 | #708 | 150 | M |
| Dec 9 | #709 | 20 | C |
| Dec 29 | #713 | 150 | M |
| Dec 30 | #715 | 260 | M |
| Dec 31 | #715 | 350 | M |
| Jan 1 | #715 | 220 | M |
| Jan 2 | #715 | 180 | X |
| Jan 4 | #715 | 130 | C |
| Jan 10 | #719 | 100 | M |
| Jan 14 | #718 | 160 | C |
| Jan 15 | #720 | 1540 | M |
| Jan 16 | #720 | 1620 | X |
| Jan 17 | #720 | 1630 | M |
| Jan 18 | #720 | 1460 | X |
| Jan 19 | #720 | 1400 | M |



During the 75 day time period covered by this table, there were a total of (720-696=) 24 catalogued sunspots. The table shows only those catalogued sunspots that were active in producing flares during this time. Sunspot areas are in terms of millionths of the solar hemisphere area, so '1630' means 0.163% of the Sun's face. Earth's area = 169 millionths by comparison!

Sunspot and solar flare data from NOAA SWN data archive at <http://www.sec.noaa.gov/Data/index.html>

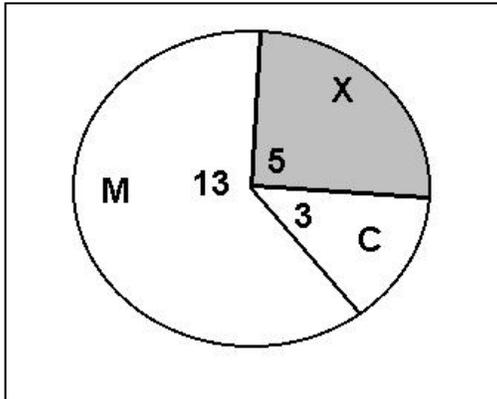
Question 1: Construct a pie chart for the X, M and C-class flare data. During this 75-day period, what percentage of flares are X-class?

Question 2: What percentage of sunspots produce X-class flares?

Question 3: What percentage of sunspots did not produce any flares during this time?

Question 4: What seems to be the minimum size for a sunspot that produces an X-class flare? An M-class flare? A C-class flare?

Question 5: If the area of Earth is '169' in the sunspot units used in the above tables, what are the maximum and minimum size of the sunspots compared to the area of Earth?



Note, there are 21 flares in the table.

X = 5 flares

M = 13 flares

C = 3 flares.

The pie chart angles are

21 = 360 degrees

$X = (5/21) \times 360 = 86$ degrees

$M = (13/21) \times 360 = 223$ degrees

$C = (3/21) \times 360 = 51$ degrees.

And to check: $223 + 86 + 51 = 360$.

Question 1: With a pie chart, what percentage of flares were X-type?

Answer: 5 out of 21 or $(5/21) \times 100\% = 24\%$

Question 2: During this 75-day period, what percentage of flares are X-class flares?

Answer: There are 24 sunspots in the sample because the catalog numbers run from 720 to 698 as stated in the table caption (A 'reading to be informed' activity). There were three sunspots listed in the table that produced X-class flares: #696, #715, #720. The percentage is $(3/24) \times 100\% = 12.5\%$ which may be rounded to 13%.

Question 3: What percentage of sunspots did not produce flares during this time?

Answer: There were only 8 sunspots in the table that produced flares, so there were 16 out of 24 that did not produce any flares. This is $(16/24) \times 100\% = 67\%$. An important thing for students to note is that MOST sunspots do not produce any significant flares.

Question 4: What seems to be the minimum size for a sunspot that produces an X-class flare? An M-class flare? A C-class flare?

Answer: Students may reasonably answer by saying that there doesn't seem to be any definite correlation for the X and M-class flares! For X-class flares, you can have them if the area is between 180 and 1620. For M-class flares, spots with areas from 130 to 1630 can have them. The two possibilities overlap. For C-class flares, they seem to be most common in the smaller spots from 20 – 130 in area, but the sample in the table is so small we can't really tell if this is a genuine correlation or not. Also, we have only shown in the table the largest flares on a given day, and smaller flares may also have occurred for many of these spots.

Question 5: If the area of Earth is '169' in the sunspot units used in the above tables, what are the maximum and minimum size of the sunspots compared to the area of Earth?

Answer: The smallest spot size occurred for #709 with an equivalent size of $(20/169) \times 100\% = 11\%$ of Earth's area. The largest spot was #720 with a size equal to $(1630/169) = 9.6$ times Earth's area.

Satellite technology is everywhere! Right now, there are over 1587 working satellites orbiting Earth. They represent over \$160 billion in assets to the world's economy. In the United States alone, satellites and the many services they provide produce over \$225 billion every year. But satellites do not work forever. Typically they have to be replaced every 10 to 15 years as new services are created, and better technology is developed. Satellites in the lowest orbits, called Low Earth Orbit (LEO) orbit between 300 to 1000 kilometers above the ground. Because Earth's atmosphere extends hundreds of kilometers into space, LEO satellites eventually experience enough frictional drag from the atmosphere that at altitudes below 300 km, they fall back to Earth and burn up. The table below gives the number of LEO satellites that re-entered Earth's atmosphere, and the average sunspot number, for each year since 1969.

| Year | Sunspots | Satellites |
|------|----------|------------|
| 2004 | 43 | 19 |
| 2003 | 66 | 31 |
| 2002 | 109 | 38 |
| 2001 | 123 | 41 |
| 2000 | 124 | 37 |
| 1999 | 96 | 25 |
| 1998 | 62 | 30 |
| 1997 | 20 | 21 |
| 1996 | 8 | 22 |
| 1995 | 18 | 20 |
| 1994 | 31 | 17 |
| 1993 | 54 | 28 |
| 1992 | 93 | 41 |
| 1991 | 144 | 40 |
| 1990 | 145 | 30 |
| 1989 | 162 | 45 |
| 1988 | 101 | 33 |
| 1987 | 29 | 13 |
| 1986 | 11 | 16 |
| 1985 | 16 | 17 |
| 1984 | 43 | 14 |
| 1983 | 65 | 28 |
| 1982 | 115 | 19 |
| 1981 | 146 | 32 |
| 1980 | 149 | 41 |
| 1979 | 145 | 42 |
| 1978 | 87 | 33 |
| 1977 | 26 | 18 |
| 1976 | 12 | 16 |
| 1975 | 14 | 15 |
| 1974 | 32 | 21 |
| 1973 | 37 | 14 |
| 1972 | 67 | 12 |
| 1971 | 66 | 19 |
| 1970 | 107 | 25 |
| 1969 | 105 | 26 |

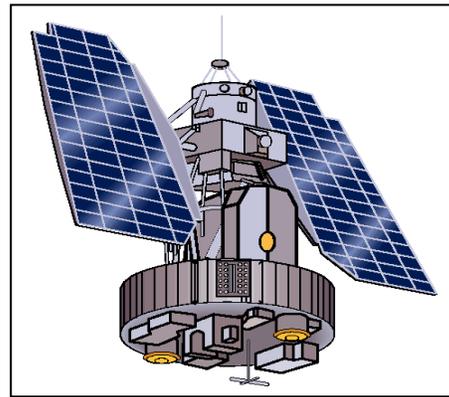


Figure: A typical weather satellite

Question 1: On the same graph, plot the number of sunspots and decayed satellites (vertical axis) for each year (horizontal axis). During what years did the peaks in the sunspots occur?

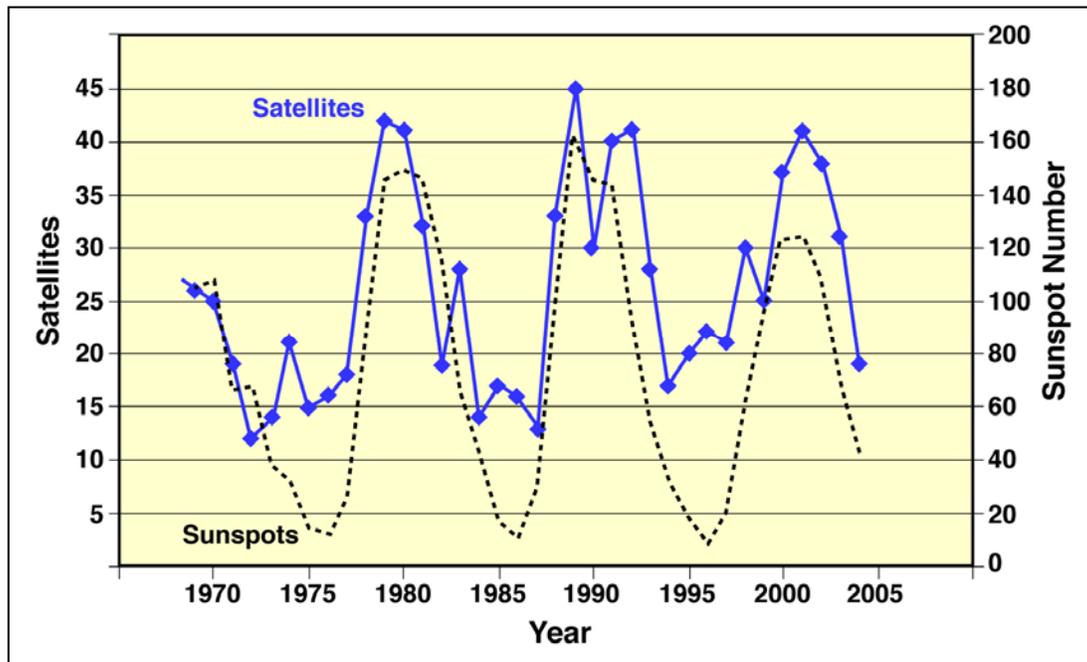
Question 2: When did the peaks in the satellite re-entries occur?

Question 3: Is there a correlation between the two sets of data?

Question 4: If you are a satellite operator, should you be concerned about the sunspot cycle?

Question 5: Do some research on the topic of how the sun affects Earth. Can you come up with at least two ways that the sun could affect a satellite's orbit?

Question 6: Can you list some different ways that you rely on satellites, or satellite technology, during a typical week?



Question 1: On the same graph, plot the number of sunspots (divided by 4) and decayed satellites for each year. During what years did the peaks in the sunspots occur? **Answer:** From the graph or the table, the 'sunspot maximum' years were 2000, 1989, 1980 and 1970.

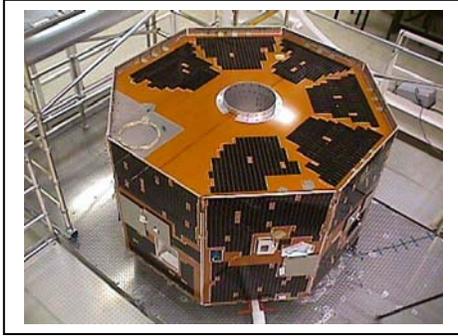
Question 2: When did the peaks in the satellite re-entries occur? **Answer:** The major peaks occurred during the years 2001, 1989, 1979 and 1969.

Question 3: Is there a correlation between the two sets of data? **Answer:** A scientist analyzing the two plots 'by eye' would be impressed that there were increases in the satellite decays that occurred within a year or so of the sunspot maxima years. This is more easy to see if you subtract the overall 'trend' line which is increasing from about 10 satellites in 1970 to 20 satellites in 2004. What remains is a pretty convincing correlation between sunspots numbers and satellite re-entries.

Question 4: If you were a satellite operator, should you be concerned about the sunspot cycle? **Answer:** Yes, because for LEO satellites there seems to be a good correlation between satellite re-entries near the times of sunspot maxima.

Question 5: Do some research on the topic of how the sun affects Earth. Can you come up with at least two ways that the sun could affect a satellite's orbit? **Answer:** The answers may vary, but as a guide, space physicists generally believe that during sunspot maxima, the sun's produces more X-rays and ultraviolet light, which heat Earth's upper atmosphere. This causes the atmosphere to expand into space. LEO satellites then experience more friction with the atmosphere, causing their orbits to decay and eventually causing the satellite to burn-up. There are also more 'solar storms', flares and CMEs during sunspot maximum, than during sunspot minimum. These storms affect satellites in space, causing loss of data or operation, and can also cause electrical blackouts and other power problems.

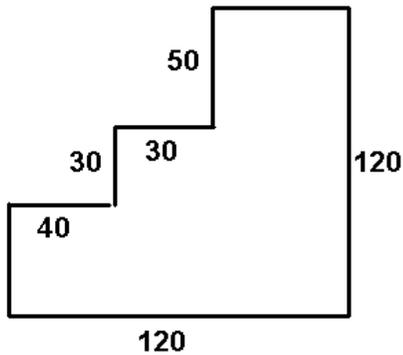
Question 6: Can you list some different ways that you rely on satellites, or satellite technology, during a typical week? **Answer:** Satellite TV, ATM banking transactions, credit card purchases, paying for gas at the gas pump, weather forecasts, GPS positions from your automobile, news reports from overseas, airline traffic management, tsunami reports in the Pacific Basin, long distance telephone calls, internet connections to pages overseas.



Solar Electricity.

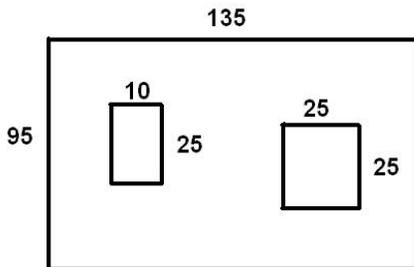
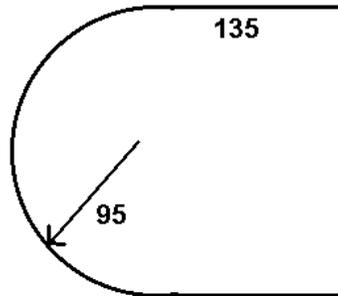
Most satellites depend on sunlight converted into electricity and stored in batteries, to run their instruments. Typical research satellites operate with only 200 to 800 watts of electricity generated by sunlight and 'solar cells'. Solar cells can be attached directly to the outer surface of a satellite, or can be found on 'solar panels' that the satellite deploys after it reaches its orbit. Engineers decide how many solar cells are needed by finding out how much power the satellite needs to operate, and then figuring out what the satellite's surface area is. If the satellite is not big enough, additional solar panels may be needed to supply the electricity. In this exercise, you will calculate the perimeter of the satellite area in centimeters, and the area, in square centimeters, of several kinds of satellite surfaces, and decide if there is enough available surface to supply the electrical needs of the satellite. All measurements in the diagrams are in centimeters. Some dimensions are missing.

The outside surface of the NASA, IMAGE satellite is covered with solar cells (black) to collect sunlight and generate electricity for its many instruments and systems.

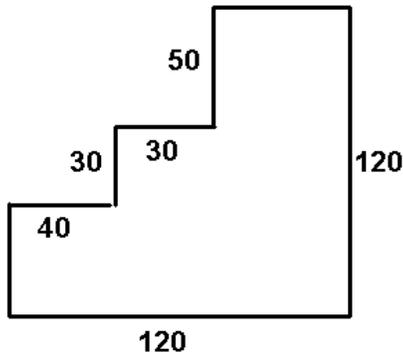


Question 1 – What is the perimeter? The area? The solar cells can provide 0.03 watts per square centimeter, and the satellite needs 257 watts. Is there enough surface area in the figure to the left to meet the electrical needs?

Question 2 - What is the perimeter? The area? The solar cells can provide 0.03 watts per square centimeter, and the satellite needs 957 watts. Is there enough surface area in the figure to the right to meet the electrical needs?



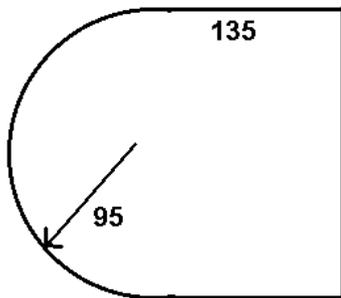
Question 3 - What is the outside perimeter? The area with the two holes removed? The solar cells can provide 0.03 watts per square centimeter, and the satellite needs 759 watts. Is there enough surface area in the figure to the left to meet the electrical needs?



Answer 1 a) The missing side can be reconstructed from the other measurements. The perimeter is $P = (120 + 120 + 50 + 50 + 30 + 30 + 40 + 40) =$
Perimeter = 480 centimeters.

B) The area can be found from breaking the figure into rectangular sections from right to left:
 $\text{Area} = (120 \times 50) + (30 \times 70) + (40 \times 40) =$
 $6000 + 2100 + 1600 =$ **9,700 square cm.**

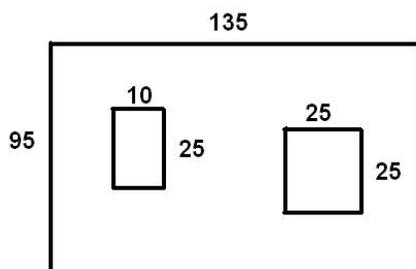
C) The solar cells produce 0.03 watts per square cm, so the power available is $9,700 \times 0.03 =$ **291 watts.**
 This is greater than the minimum satellite requirement of 257 watts.



Answer 2 a) From the radius of the half-circle, the rectangle has a length of $2 \times 95 = 190$ cm, so the sum of the three sides is 460 cm. The circumference of the semi-circle is $(3.14) \times 95 = 298.3$ cm. **Perimeter = 758.3 centimeters.**

B) The area can be found from breaking the figure into a rectangle and a semi-circle.
 $\text{Area} = (135 \times 190) + \frac{1}{2} (3.14) (95)^2 =$
 $25,650 + 14,169 =$ **39,819 square cm.**

C) The solar cells produce 0.03 watts per square cm, so the power available is $39819 \times 0.03 =$ **1194 watts.**
 This more than the minimum satellite requirement of 957 watts.

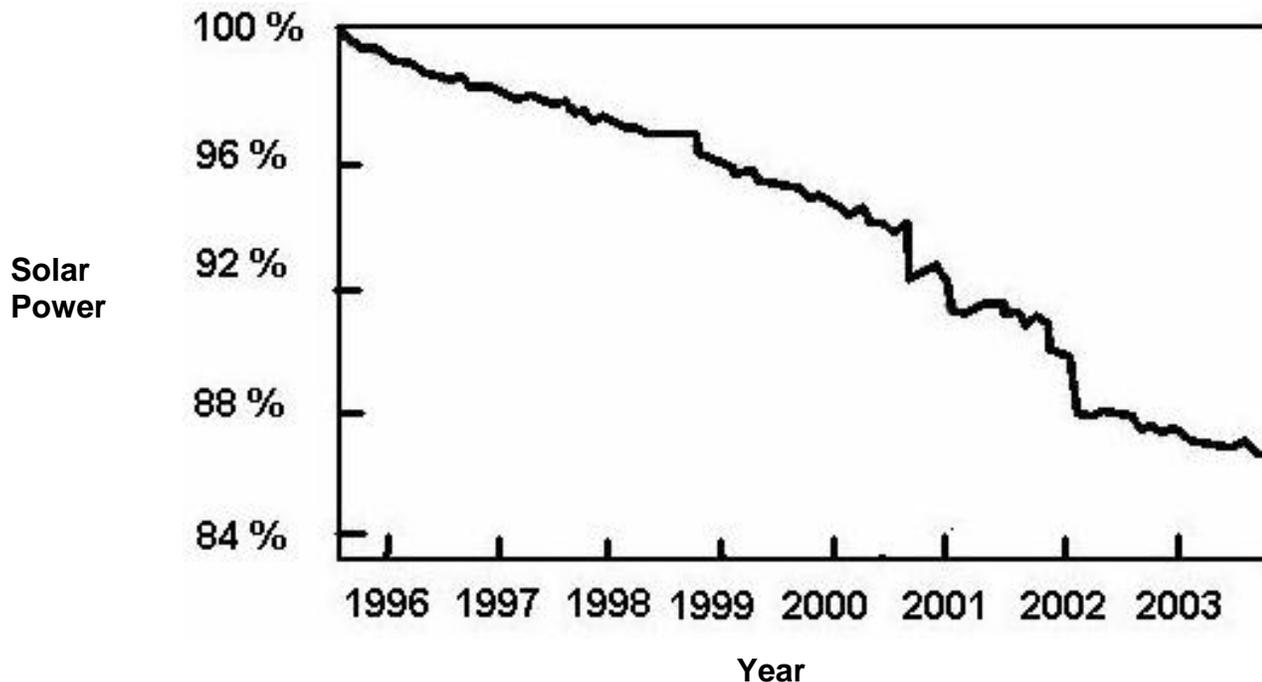


Answer 3 – a) The perimeter is $P = (135 + 135 + 95 + 95) =$ **460 centimeters.**

B) Calculate the area of the large rectangle and subtract the two interior holes: $135 \times 95 - 10 \times 25 - 25 \times 25$
 $12825 - 250 - 625 =$ **11,950 square cm.**

C) The solar cells produce 0.03 watts per square cm, so the power available is $11950 \times 0.03 =$ **358 watts.**
 This less than the minimum satellite requirement of 759 watts.

Soon after the first satellites were placed into orbit, engineers began to notice that the electrical power needed to operate the satellites was slowly declining. Very careful studies of the way that solar cells worked in space soon came up with a culprit: Cosmic rays! Cosmic rays are very high-speed ions, protons and electrons that travel through space. Some are produced by the sun during solar flares, while others come from space beyond the solar systems itself. Cosmic rays are deflected by strong magnetic fields. Fortunately, Earth has a very strong magnetic field that shields us from most of these cosmic rays, but enough get through that they collide with solar panels and solar cells on satellites orbiting Earth. Over time, these fast-moving particles cause changes in solar cells, making them less able to generate the electricity they are supposed to when sunlight falls on them. Thanks to decades of study, engineers can make very accurate models of these cosmic rays effects and incorporate them into the design of satellite power systems. Below is an actual graph prepared by Dr. Paul Brekke, the Project Scientist for the Solar Heliospheric Observatory. It shows how fast the satellite's solar arrays have changed their power output since 1995.

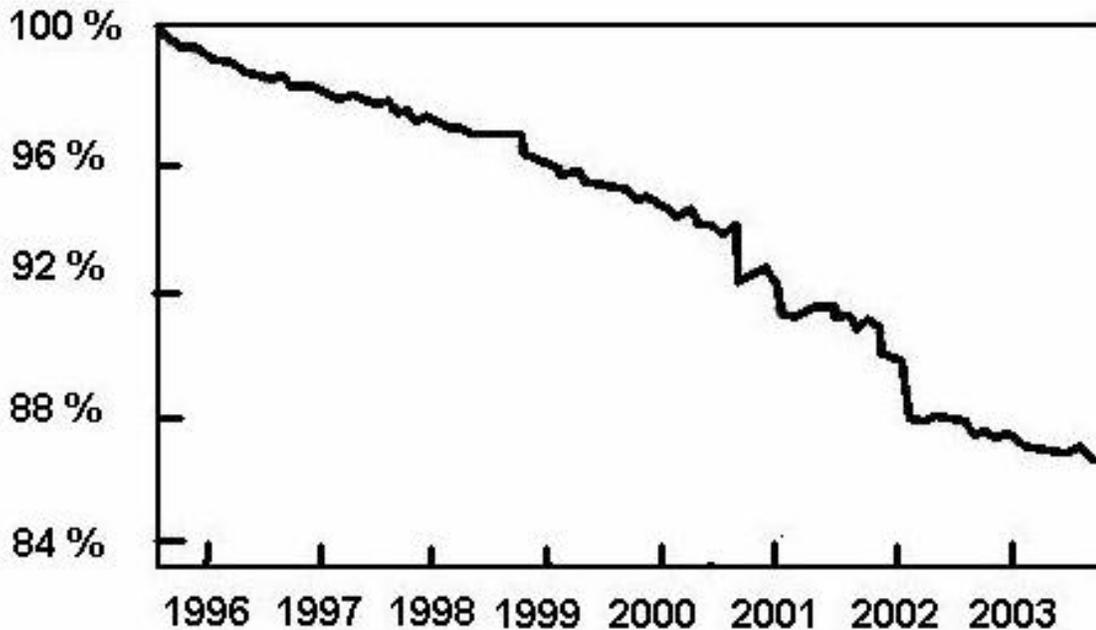


Question 1: By how much has the SOHO satellite power declined by 2002?

Question 2: Satellites often remain usable for 15 years. By what percentage will the electricity from the SOHO solar panels have declined by that time?

Question 3: The instruments on a satellite require 850 watts of power to operate. If a scientist wants her instrument to continue working for 15 years, how large should the satellite power supply be at the time of launch?

Question 4: The surface of a satellite has an area of 1000 square centimeters. The solar cells can generate about 0.03 watts per square centimeter. A) What is the total power available to the satellite by covering its surface with solar cells? B) If the satellite is to last 15 years, what is the maximum power that the instruments can draw and still work after 15 years?



Question 1: By how much has the SOHO satellite power declined by 2002?

Answer: From the plot, the power has declined to 88% of its original 100% at launch.

Question 2: Satellites often remain usable for 15 years. By what percentage will the electricity from the SOHO solar panels have declined by that time? **Answer:** From the previous answer, the decline was 12% in 6 years, so after 15 years the decline will be $(15/6) \times 12\% = 30\%$.

Question 3: The instruments on a satellite require 850 watts of power to operate. If a scientist wants her instrument to continue working for 15 years, how large should the satellite power supply be at the time of launch? **Answer:** From the previous answer, if the experiments need 850 watts to operate after 15 years, the solar panels have to be designed to produce 30% more than 850 watts at the start of the mission or $(1.30) \times 850$ watts = 1105 watts.

Question 4: The surface of a satellite has an area of 1000 square centimeters. The solar cells can generate about 0.03 watts per square centimeter. A) What is the total power available to the satellite by covering its surface with solar cells? B) If the satellite is to last 15 years, what is the maximum power that the instruments can draw and still work after 15 years?

Answer:

A) The total power will be 3000 square cm \times 0.03 watts per square cm = 90 watts.

B) Because the solar panels will degrade by 30% during the 15 years, this means that after 15 years you will only have 90 watts \times 0.70 = 63 watts to run your instruments!!

Scientists typically take advantage of the surplus of energy at the start of a mission to run the most energy-consuming instruments, then shut them down one at a time until the satellite finally stops being a useful scientific instrument.

Scientists have to use mathematics to analyze data, and to build models of the phenomena they are studying. Can you solve this crossword puzzle using the mathematical clues provided? When you're finished, color the blank squares with your favorite aurora colors!

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Extra Credit Problem

Word Bank:

| | | | |
|--------------|------------|------------------|------------------|
| +4 proton | - 14 RPI | +6 ionosphere | -1 plasma |
| -16 FUV | 11 photons | +27 spectrum | -27 beams |
| +3 radiation | 0 flares | -10 field | -7 magnetism |
| -6 earth | -8 solar | -13 envelope | -2 current |
| -3 aurora | - 23 cone | +2 corona | 10 humanity |
| +1 rays | 13 oval | -11 Plasmasphere | -26 echos |
| -9 polarity | +23 STP | -17 CMEs | +26 UT |
| +19 TOD | 9 ions | -19 sunspot | +25 ENA |
| -21 FAC | -5 IMAGE | -4 neutron | +8 electrons |
| +14 watt | 17 UV | +7 crown | +5 magnetosphere |

The numerical answer to each problem below will tell you which word to use in the word bank to fill in the row or column with the indicated letter.

Down:

l) $- 2 (- 5 + 3)$

r) $- 3 (- 12 + 9)$

m) $- 4 (3 - 1)$

T) $+ 2 - 3 + 5 - 10 + 2$

e) $+ 2 (- 6 + 3) + 4$

u) $+ 4 (- 5 + 3) - (- 7 + 6)$

n) $- 3 (- 5 + 2) + (- 4 + 3)$

v) $+ 3 (- 8 + 6) - 3$

g) $+ 5 - (- 8 + 2)$

x) $+ 4 (8 - 3) - 3 (+ 6 - 8 + 12)$

o) $- 4 (7 - 3) + (8 - 3)$

y) $+ 2 (+ 8 - 5 + 10) - (+ 10 + 5 - 2)$

p) $+ 1 - 1 + 3 + 4 - 5 - 8$

J) $- 2 (- 3 + 2 - 5 - 6) + 2 - 2 (+ 26)$

Across:

a) $+ 2 (- 3 + 8) - 5$

g) $(+ 1 - 1) + (+ 1 - 2)$

b) $+ 3 (+ 2 + 1) - 2 (- 3 + 9)$

h) $+ 4 (+ 5 - 2) - 3 (+ 3)$

c) $- 15 (- 2 + 3) + 3 (- 2 + 9)$

k) $+ 5 (+ 8 - 5) - 4 (- 6 + 8)$

d) $- 1 + 1 - 1 + 1 - 1 + 1$

s) $- 1 + 1 - 1 + 1 + 1 - 1 + 1$

e) $- 6 + (+ 11 - 3)$

w) $+ 3 (- 2 + 8) + (- 12 + 4)$

f) $- 3 (- 8 + 11) + 4$

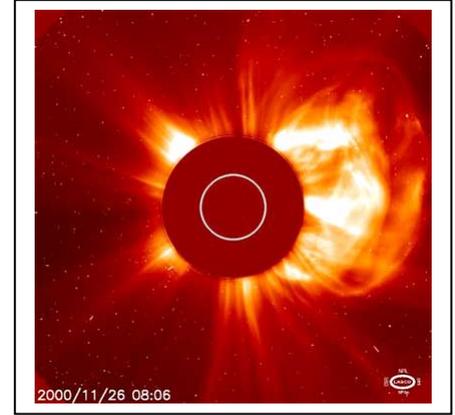
z) $- 5 + 2 (- 8 + 4)$

A Bird's-Eye Look at the Sun-Earth System

Solar flares are powerful releases of energy in the tangled **A_magnetic fields** of the sun, thousands of kilometers above certain sunspots. Within a few minutes, these **B_____** attempt to reconnect themselves into simpler shapes, releasing their stored energy. This energy heats the local **C_____** to millions of degrees, producing tremendous blasts of x-ray and gamma ray energy. Within 8.5 minutes, this **D_____** energy can reach Earth and disrupt the ionosphere. The **E_____** is the region of our atmosphere where radio waves can be reflected back to the ground so that we can send radio programs and messages around the world. But during **F_____**, radio broadcasting can be shut down for hours.

Scientists eventually discovered that, in addition to flares, discharges of plasma from the sun could also occur. With satellite sensors in space, they eventually caught sight of how the sun could from time to time release billions of tons of plasma traveling at millions of miles per hour. When these magnetized plasma clouds wash across Earth's magnetic field – called the **G_____**, these clouds can dump huge amounts of matter and energy into Earth's environment. **H_____** and magnetic storms are often the consequence of these **I_____**.

The entire Earth-Sun system follows a complicated give-and-take when severe solar **J_____** occur. Earth counteracts this onslaught of plasma and energy by a complex series of adjustments only available to it because it has a powerful magnetic field. With the magnetic field, most of the solar storm energy is diverted. What little enters the magnetosphere eventually finds its way into circulating **K_____** which return some, but not all of the magnetospheric plasma back to the solar wind – a constant stream of matter that leaves the solar surface. Solar storms cause Earth's magnetic field to be pulled into the shape of a **L_____**. The distant **M_____** can snap like pulled taffy as it attempts to relieve the magnetic stresses building up in the system. The released energy causes currents of **N_____** to flow into the upper atmosphere where they collide with atoms of oxygen and nitrogen to produce the spectacular displays of the Aurora Borealis and **O_____**.



Coronal Mass Ejection (CME) seen by SOHO satellite.

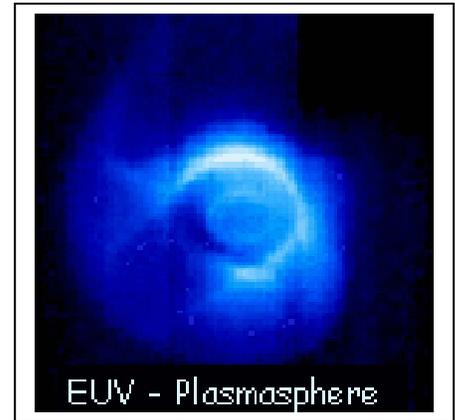


IMAGE sees Earth's upper atmosphere – the Plasmasphere.

| | | |
|-------------------|----------------------------|---------------------------|
| -4 = Ring current | -9 = ionosphere | 4 = electromagnetic |
| 0 = Magnetotail | -3 = solar flares | 10 = oxygen |
| 3 = Plasma | 8 = corona | 1 = Coronal Mass Ejection |
| -7 = Sunspot | -1 = magnetosphere | -11 = stratosphere |
| 2 = Aurora | 11 = atmosphere | 12 = plasmasphere |
| -10 = Ozone layer | 6 = magnetic fields | 5 = Aurora Australis |
| -6 = Comet | 9 = sphere | -8 = photosphere |
| 7 = Fields | -2 = storms | -5 = charged particles |

Extra Credit Problem

10

Solve these equations for X to find the number in the Word Bank. Write the word on the indicated lettered line in the essay, then answer the questions below.

A $(x - 2) - 4 = 0$ **Answer: x= 6. From Word Bank 6 = 'magnetic fields'**

B $2(3-x) + 8 = 0$

C $8x - 2(2x - 4) + 4(4 - 3x) = 0$

D $-3x + 4 = 5x - 28$

E $-15 - 2x = 3(x + 10)$

F $4x - 4 - (3x - 4) + 3 = 0$

G $-(2x - 3) - (8 + 3x) = 0$

H $-(4x - 18) + 4(4 - 2x) - 2(3x-1) = 0$

I $-(3-4x) + 2(5-6x) - 6 = 3(2x - 5) - (x-3)$

J $-(2x + 8) + 6x = -16$

K $3(2x + 10) + 3x + 6 = 0$

L $-x + 3(2x - 5) + 3x = 2x - 51$

M $-x + 5 + (3x - 2) + 6 = 3(x + 3) - 2x$

N $-6(x+5) = 0$

O $5(x + 5) + 10(x - 3) = 70$

Question 1: Do the particles that cause aurora come from Earth's environment or directly from the Sun?

Question 2: What is a Coronal Mass Ejection?

Question 3: What roles do magnetic fields play in causing disturbances on the sun and Earth?

Question 4: Where does the energy come from to cause solar storms and aurora?

Question 5: How does Earth's magnetic field prevent solar storms from reaching the atmosphere?

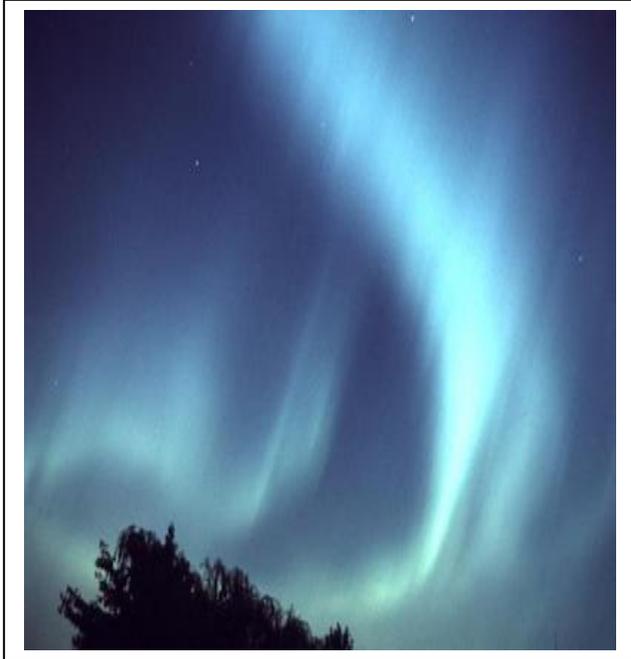
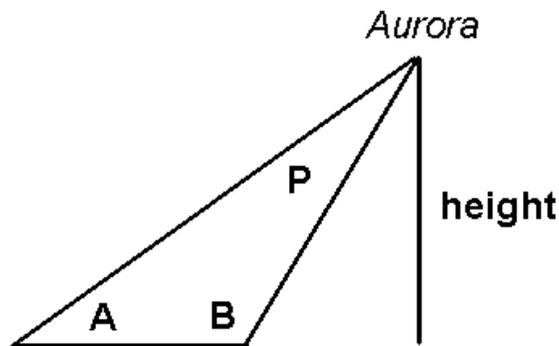


Image courtesy Tim Tomljanovich, <http://www.nsaclub.org/photos/aurora/>

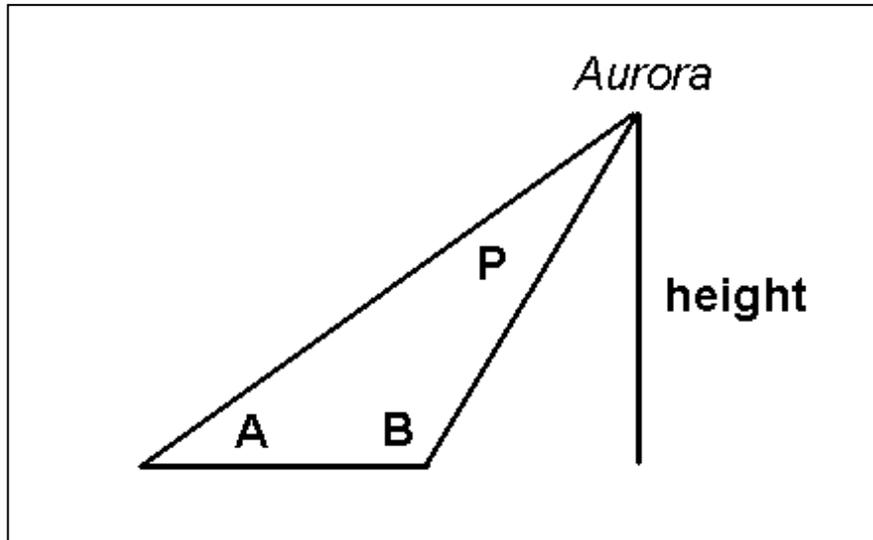
For thousands of years, people living at northern latitudes had no idea how high up the Aurora Borealis was located. Before the advent of photography in the 1880's, auroral observers tried to determine the height of aurora by the method of triangulation. One of the earliest of these measurements was made by the French scientist Jean-Jacques d'Ortous de Mairan between 1731 and 1751. From two stations 20 km apart, observers measured the angles A and B between the ground and a specific spot on an aurora. From the geometry of the triangle, they estimated that aurora's height was between 650 - 1,000 km above the ground. More precise measurements yielded estimates from 70 to 200 kilometers.



Question 1 - Suppose that two observers were located 30 kilometers apart. Observer A measured an angle of 53 degrees and Observer B measured an angle of 114 degrees. By making a scaled drawing of this triangle, what was the height of the auroral feature they were studying?

Question 2 - Use a protractor to measure the vertex angle, P. What happens to the measurement of angle P if you decrease the 'baseline' distance between the observers to 5 kilometers?

Question 3 – What would the measurements of the two angles be if the aurora were located over a spot half-way between the two observers?



Question 1 - Suppose that two observers were located 30 kilometers apart. Observer A measured an angle of 53 degrees and Observer B measured an angle of 114 degrees. By making a scaled drawing of this triangle, what was the height of the auroral feature they were studying?

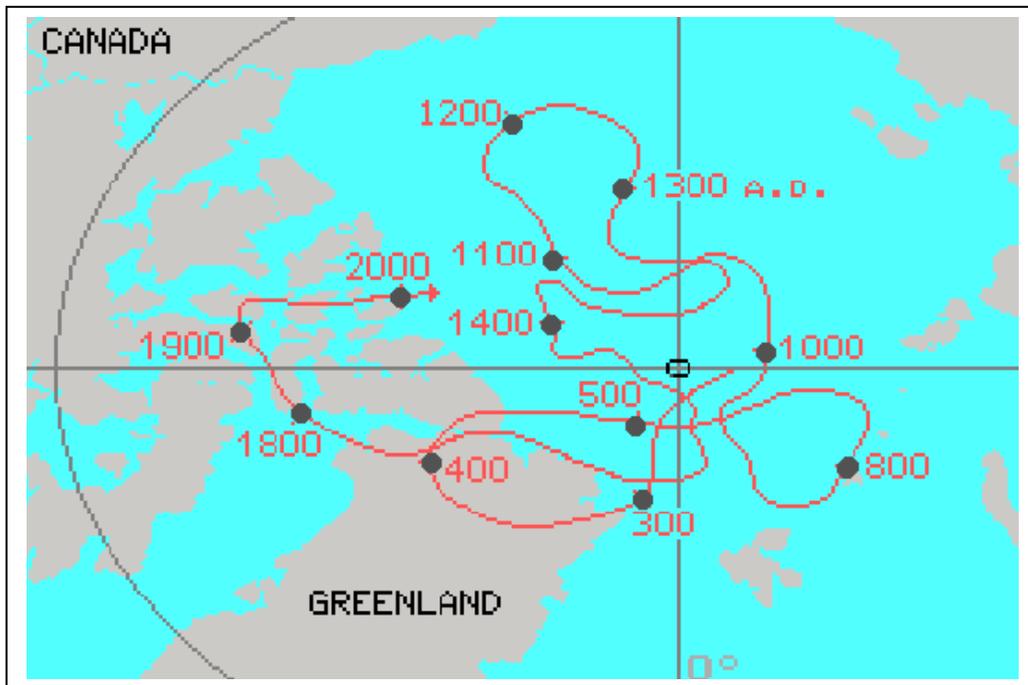
Answer: Students should get an answer near 100 kilometers.

Question 2 - Use a protractor to measure the vertex angle, P. What happens to the measurement of angle P if you decrease the 'baseline' distance between the observers to 5 kilometers?

Answer: The angle P should have a measure of $180 - 114 - 53 = 13$ degrees. If the baseline is decreased to 5 kilometers with Observer A moving towards Observer B and Observer B remaining at the previous location, Observer B will measure an angle of 114 degrees, Observer A will measure 64 degrees, angle P will decrease to $180 - 114 - 64 = 2$ degrees. This is a very small angle to accurately measure.

Question 3 – What would the measurements of the two angles be if the aurora were located over a spot half-way between the two observers who are 30 kilometers apart?

Answer : From a scaled drawing $A = B = 80$ degrees.



The Earth's magnetic North Pole moves around quite a bit, especially if you plot its position during the last 1700 years! The scale of the above plot is approximately 380 km per centimeter. Use this scale and a piece of string and the dates for each position, to answer the following questions:

Question 1: What is the total distance that the North Magnetic Pole wandered from 300 AD to 2000 AD?

Question 2: What is the shortest distance that the pole wandered in a 100-year period?

Question 3: What is the longest distance that the pole wandered in a 100-year period?

Question 4: What is the average speed of the wander from 300 AD to 2000 AD?

Question 5: What is the fastest speed it traveled in a 100-year period?

Question 6: Is the speed of the wander during the last 100 years unusual compared to the average speed or to the fastest speed?

This exercise introduces students to the idea that Earth's magnetic poles are not fixed in space and time. Since the 1700's, mapmakers have known that the bearings to seaports and other fixed landmarks change in a steady manner from decade to decade so that maps often have to be re-drawn to reflect the new bearings. Geologists call this phenomenon 'polar wander'. (It has nothing to do with Earth's rotation axis!!)

Students will be asked to study a map of the wandering magnetic North Pole and answer some quantitative questions. To measure the distance (along the red track) that the magnetic pole has wandered, have students use a piece of string laid along the track, and then measure the length of the track in centimeters. The scale of their map is about 380 km/cm, so multiplying the string length by this scale factor, they can easily compute the track length and answer the questions. Students will also need to compute the speed of the pole movement between the years indicated on the map, by dividing the relevant track interval they measured by the difference in the years.

Question 1 - What is the total distance that the North Magnetic Pole wandered from 300 AD to 2000 AD? **Answer:** The string was 48 cm long which equals $48 \text{ cm} \times 380 \text{ km/cm} = 18,240 \text{ km}$.

Question 2 - What is the shortest distance that the pole wandered in a 100-year period? **Answer:** Between 500 and 800 AD the string measured 4 cm or 1520 km. The time interval is 3 centuries, so in 1 century the pole traveled $1520/3 = 507 \text{ km}$.

Question 3 - What is the longest distance that the pole wandered in a 100-year period? **Answer:** The longest distance is between 1300 and 1400 AD for a length of 6.5 cm or 2470 km

Question 4 - What is the average speed of the wander from 300 AD to 2000 AD? **Answer:** Average speed is the distance divided by time = $18,240 \text{ km}/1700 \text{ years}$ or 11 km/year.

Question 5 - What is the average fastest speed it traveled in a 100-year period? **Answer:** Between 1300 and 1400 it traveled 2470 km in 100 years or 24.7 km/year!

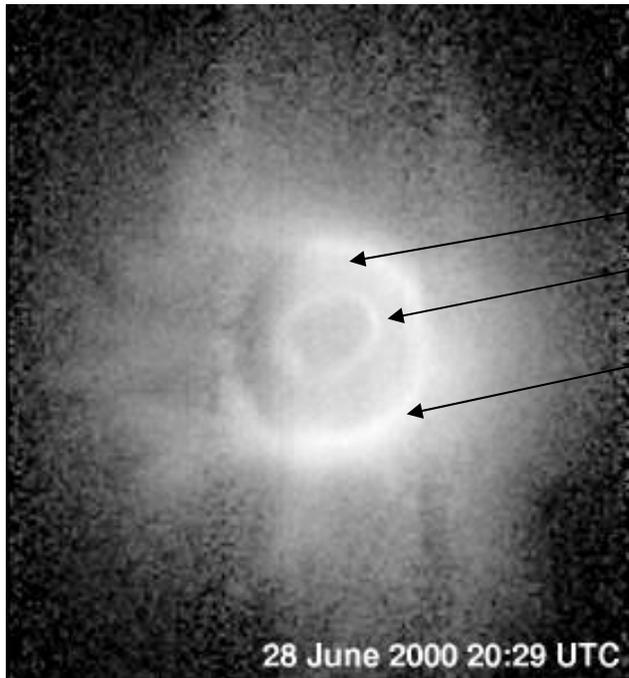
Question 6 - Is the speed of the wander during the last 100 years unusual compared to the average speed or to the fastest speed? **Answer:** $2.5 \text{ cm} = 960 \text{ km}$ so $960 \text{ km}/100 \text{ yrs} = 9.6 \text{ km/year}$. It's slightly below average but not a record-holder!

Note to teachers: If you have the students calculate the average speeds for each 100-year period and plot this on a speed vs year graph, the students will see that the polar wander represents accelerated motion because the speed is not constant from century to century!

The Plasmasphere.

Most people, when asked, would say that the atmosphere of Earth probably comes to an end a few hundred kilometers above the surface of Earth. In fact, our atmosphere has been detected more than 10,000 kilometers above the surface. This region of very dilute gas is called the Plasmasphere because the atoms are often ionized by the very harsh ultraviolet light from the sun. This kind of gas is called a plasma. Wherever the ultraviolet light reaches the plasmasphere's gas, the gas glows and can be photographed with special equipment.

The image below was taken by the IMAGE EUV instrument on June 28, 2002 at 4:09 PM (EDT). It shows the plasmasphere as revealed by the glow of ionized helium atoms at a wavelength of 121.6 nanometers (1216 Angstroms). Additional 'still' images and movies can be retrieved at the IMAGE satellite's EUV instrument website at the University of Arizona (<http://euv.lpl.arizona.edu/euv/>)



The image was taken above the North Pole. Helium atoms excited by the ultraviolet light from the sun give off a special wavelength of light that the IMAGE instrument can detect.

The round disk in the center is Earth.

The smaller, irregular oval-shaped ring is the ring of aurora (the auroral oval).

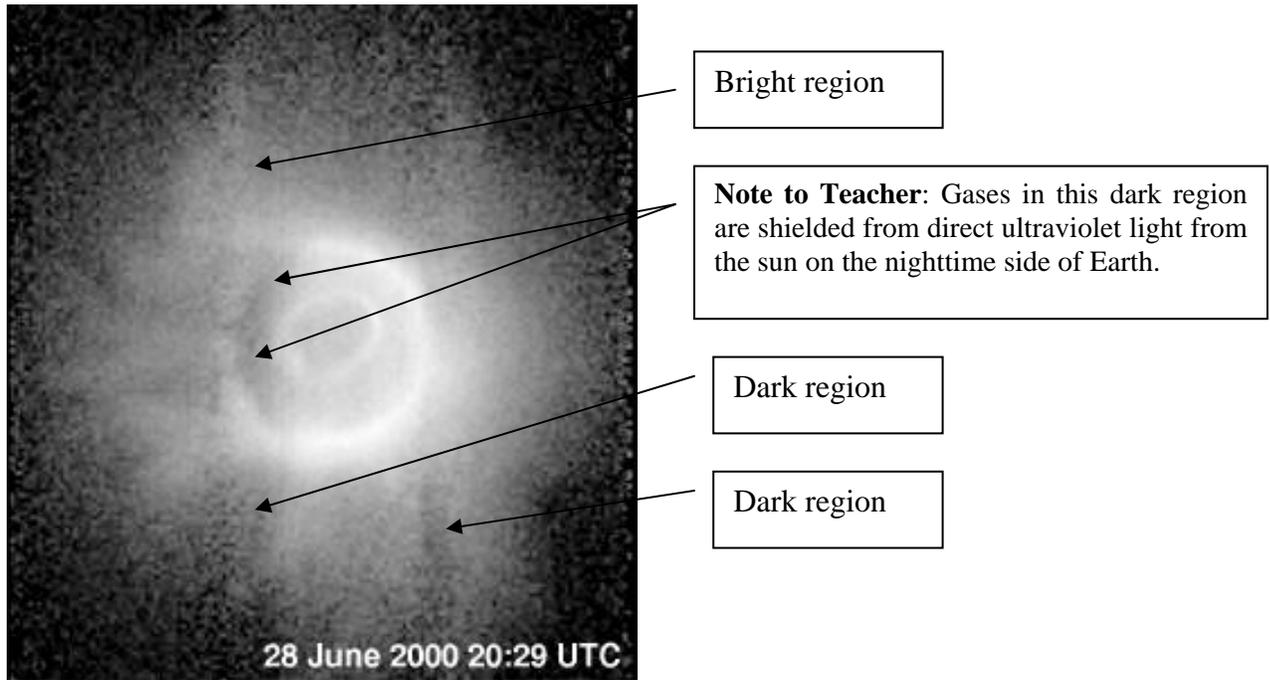
The larger ring is the glow of helium atoms in the dense part of the plasmasphere nearest Earth.

With the center of the Earth disk as the origin, use a millimeter ruler and a compass to answer the following questions:

Question 1 - Is the gas in the plasmasphere lumpy or smooth? Use the picture above to give examples that support your answer.

Question 2 - If the radius of Earth is 6,378 kilometers, what is the maximum and minimum range for the plasmasphere altitude above Earth's surface?

Question 3 - Using the scale of this image calculated from Question 2, draw circles that represent the orbits of the International Space Station (altitude 400 km), the Global Positioning Satellite system (altitude 20,200 km) and GEO communications satellites (altitude 35,900 km). Are they inside or outside the plasmasphere?



Question 1 - Is the gas in the plasmasphere lumpy or smooth? Give examples.

Answer: The gas is mostly lumpy. As examples, students can point out specific features by drawing arrows to them and describing what they see as in the examples above.

Question 2 - If the radius of Earth is 6,378 kilometers, what is the maximum and minimum range for the plasmasphere altitude above Earth's surface?

Answer: If the page is printed using normal printer defaults for enlargement, the Earth disk has a diameter of 24 millimeters. This means the image scale is $6378/12 = 530$ km/millimeter. The typical range of the plasmasphere outer edge from the edge of the earth disk is between 20 – 40 millimeters, so the physical range is $20 \times 530 = 10,600$ to $40 \times 530 = 21,200$ kilometers!

Question 3: The scale of the image is 530 km/mm.

ISS orbit = 0.8 mm from edge of Earth limb in above image.

GPS satellites = $20200/530 = 38$ mm from earth's limb.

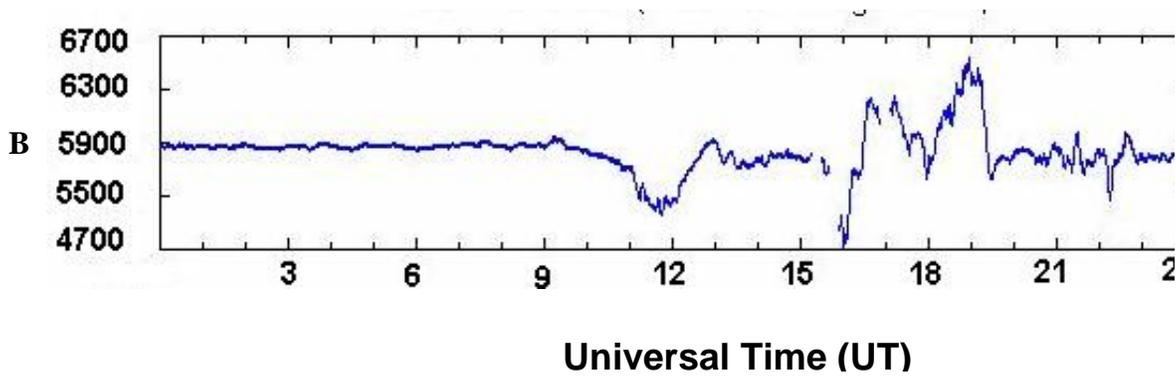
GEO satellites = 67.7 mm from Earth's limb.

The ISS and GPS satellites are inside the plasmasphere. The GEO communications satellites are just outside the plasmasphere. Students may draw circles of radii 12.8, 50, and 79.7 mm on the above image to represent the orbits.

Magnetic Storms are disturbances in Earth's magnetic field that can be detected from the ground using sensitive instruments called magnetometers. Dozens of these instruments located at 'Magnetic Observatories' around the world keep track of these disturbances. The graph below shows these changes during a 24-hour period on October 24, 2003.

The vertical axis in the plot gives the magnitude, B , of this magnetic change on Earth that is in the East to West direction. The strength of a magnet can be described in terms of a unit called a Tesla. On this plot, the vertical axis gives the magnetic strength in units of nano-Teslas (nT). One nano-Tesla is one billionth of a Tesla (so 1 billion nano-Teslas = 1 Tesla) . We can see that on this day, Earth's magnetic field varied between 4700 and 6700 nano-Teslas.

The horizontal axis is the time measured in Universal Time (UT). When scientists study events that change in time, they often use Universal Time, which is also known as Greenwich Mean Time. All scientific measurements are referred to this standard of time keeping to avoid problems converting from one time zone to another. Universal Time or 'UT' follows a 24-hour clock, so that 6:00 PM is written as 18:00 and 1:00 PM is written as 13:00. Use the time calculator at <http://www.indiana.edu/~animal/fun/conversions/worldtime.html> to convert your local time to Universal Time!



Question 1 – If a magnetometer measured a magnetic field of 137,000 nT, how many Teslas would that correspond to?

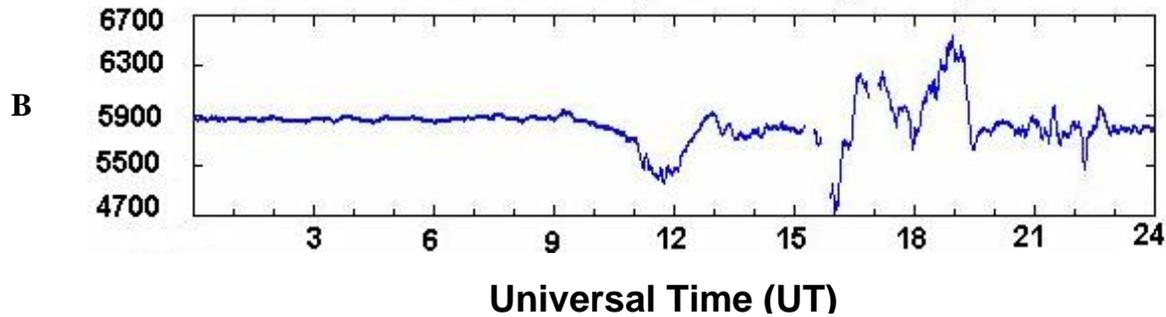
Question 2 – What is the corresponding Universal Time for 9:45 PM?

Question 3 - From the above graph, at what time was the magnetic storm most severe in terms of the absolute magnitude of its change in B ?

Question 4 – At what time did the storm episode begin and end?

Question 5 – As a percentage of 5900 nT, what was the largest change in the magnetic field?

Question 6 - How long did the magnetic storm last?



Question 1 – If a magnetometer measured a magnetic field of 137,000 nT, how many Teslas would that correspond to?

Answer :

$$\frac{137,000 \text{ nT}}{1} \times \frac{1 \text{ Tesla}}{1,000,000,000 \text{ nT}} = 0.000137 \text{ Tesla}$$

Question 2 – What is the corresponding Universal Time for 9:45 PM?

Answer : 21:45 UT.

Question 3 - From the above graph, at what time was the magnetic storm most severe?

Answer: Students should look for the largest ‘absolute magnitude’ change in the graph from the ‘average’ level of 5900 nT. That occurs at about 16:00 UT.

Question 4 – At what time did the storm episode begin and end?

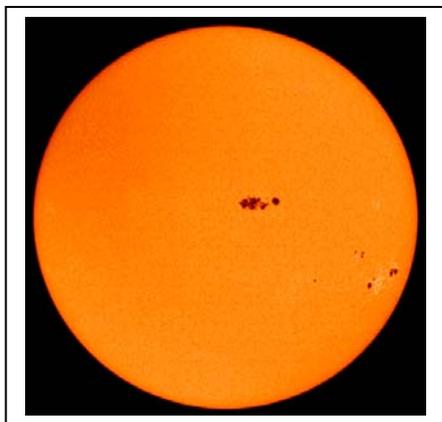
Answer: The ‘calm’ periods occurred between 00:00 and 09:00 and from 23:00 to 24:00. The storm period occurred between 09:00 and 21:00 UT

Question 5 – As a percentage of 5900 nT, what was the largest change in the magnetic field?

Answer: The largest change in terms of absolute magnitude occurred at 16:00 when the magnetic field went from 5900 nT to 4700 nT. This is a decrease of 1200 nT. As a percentage this was $(1200/5900) \times 100\% = 20\%$ from the non-storm conditions.

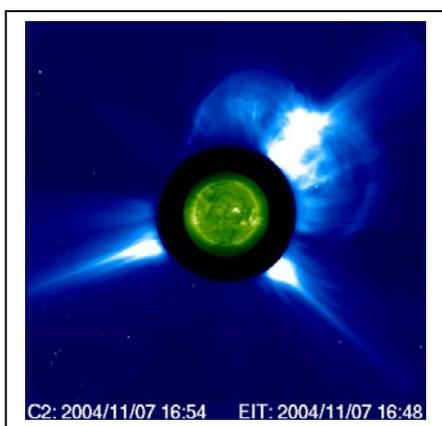
Question 6 - How long did the magnetic storm last?

Answer: The entire storm lasted $21:00 - 09:00 = 12$ hours.



November 6 - 9, 2004 were very active days for solar and auroral events. A major sunspot group, AR 0696, with a complex magnetic field produced several Coronal Mass Ejections and flares during this time. There was an X2.0-class solar flare on November 7, 16:06 UT and a CME ejection. On November 9 and 12:00 UT, the beginnings of a major geomagnetic storm started. The NOAA Space Weather Bulletin announced that:

The Geomagnetic field is expected to be at unsettled to major storm levels on 09 November due to the arrival of a CME associated with the X2.0 flare observed on 07 November. Unsettled to minor storm levels are expected on 10 November. Quiet to active levels are expected on 11 November.



Many observers as far south as Texas and Oklahoma reported seeing beautiful aurora on Sunday night from an earlier CME/flare combination on Saturday, November 6th. In the space provided below, calculate the speed of the CME as it traveled to Earth between November 7th - 9th assuming that the distance to Earth is 93 million miles, or 147 million kilometers.

Question 1 - How long did it take for the CME to arrive?

Question 2 - What is the speed of the CME in miles per hour?

Question 3 - What is the speed of the CME in kilometers per hour?

Question 4 - What is the speed of the CME in miles per second?

Question 5 - What is the speed of the CME in kilometers per second?

The distance to the Earth is 93 million miles or 147 million kilometers.
 Start time = November 7 at 16:06 UT
 Arrival time = November 9 at 12:00 UT

Question 1 - How long did it take for the CME to arrive?

Answer: November 7 at 16:06 UT to November 8 at 16:06 UT is 24 hours.
 From Nov 8 at 16:06 to Nov 9 at 12:00 UT is
 $(24:00 - 16:06) + 12:00$
 $= 7:54 + 12:00$
 $= 19 \text{ hours and } 54 \text{ minutes.}$
 Total time = 24 hours + 19 hours and 54 minutes = 43 hours and 54 minutes.

Question 2 - What is the speed of the CME in miles per second?

Answer: In decimal units, the travel time from question 1 equals 43.9 hours.
 The distance is 93 million miles so the speed is 93 million miles/43.9 hours
 Or 2.1 million miles per hour.

Question 3 - What is the speed of the CME in kilometers per second?

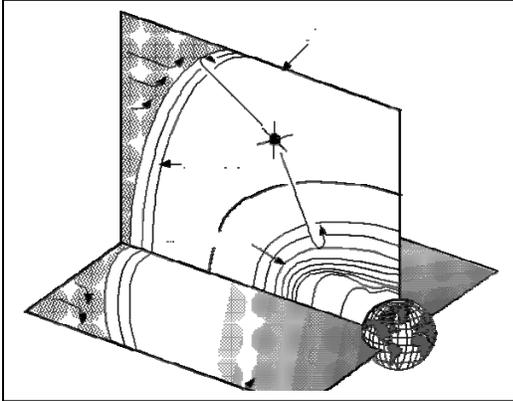
Answer: Use the conversion that 1.0 miles = 1.6 kilometers, then
 $2.1 \text{ million miles/hour} \times 1.6 \text{ km/mile} = 3.4 \text{ million kilometers per hour}$

Question 4 - What is the speed of the CME in miles per second?

Answer: Convert hours to seconds by
 $1 \text{ hour} \times 60 \text{ minutes/hour} \times 60 \text{ seconds/minute} = 3,600 \text{ seconds.}$
 Then from question 2: $2.1 \text{ million miles/hour} \text{ divided by } 3600 \text{ seconds/hour}$
 $= 583 \text{ miles/second.}$

Question 5 - What is the speed of the CME in kilometers per second?

Answer: From question 3 and the conversion of 1 hour = 3600 seconds:
 $3.4 \text{ million kilometers / second} \text{ divided by } 3600 \text{ seconds/hour}$
 $= 944 \text{ kilometers/sec.}$



The IMAGE spacecraft (shown as the 'star' in the figure) contains an instrument called the Radio Plasma Imager (RPI). This instrument sends out a powerful pulse of radio energy (the fish hook-shaped lines) at frequencies from 3,000 to 3 million cycles per second (Hertz). When the echos from these pulses are later received by the instrument, they can be analyzed to find the location and density of the plasma that reflected them.

Clouds of plasma in space have an interesting property: When radio waves reflect off of them, the radio frequency of the reflected signal depends on the density of the cloud! The formula that relates the reflection frequency, F , to the density, N , is given by

$$F = 9000 \times (N)^{1/2}$$

The unit of frequency is Hertz (cycles per second) and the unit for the density of the cloud is electrons per cubic centimeter.

In this problem, you will use some of the same methods and equations that IMAGE scientists use, to study the properties of plasma clouds near Earth. Although the properties of these clouds, and their locations, have been 'made-up' for this problem, your analysis of them will be similar to the methods employed by IMAGE scientists using real data.

With the formula above, solve for the density, N , and complete the table entries below.

| Location | Direction (degrees) | Distance in Earth Radii (R_e) | Reflection Frequency (Hertz) | Density (electrons per cc) |
|----------|---------------------|-----------------------------------|------------------------------|----------------------------|
| 1 | 300 | 1.0 | 284,000 | 995 |
| 2 | 315 | 2.5 | 201,000 | |
| 3 | 350 | 6.5 | 12,600 | |
| 4 | 45 | 4.5 | 20,100 | |
| 5 | 60 | 3.9 | 25,500 | |
| 6 | 90 | 4.1 | 28,500 | |
| 7 | 120 | 4.0 | 25,500 | |
| 8 | 135 | 5.5 | 20,100 | |
| 9 | 215 | 7.2 | 12,600 | |
| 10 | 230 | 3.5 | 220,000 | |
| 11 | 270 | 1.2 | 348,000 | |

The equation solved for N is:

$$N = (F/9000)^2$$

Lets' calculate the answer for N for the first location in Line one of the table. Divide the reflection frequency in Column 4 by 9,000. For example, at Location 1, $284,000/9,000 = 31.55$. Find the square of this number: $31.55 \times 31.55 = 995.4$. Round this number to the nearest whole number, therefore the density of the cloud, N, at Location 1 is 995 electrons per cubic centimeter. Students will enter this answer in Column 5.

Complete the rest of the entries to Column 5 in similar fashion.

| Location | Direction (degrees) | Distance in Earth Radii (Re) | Reflection Frequency (Hertz) | Density (electrons per cc) |
|----------|---------------------|------------------------------|------------------------------|----------------------------|
| 1 | 300 | 1.0 | 284,000 | 995 |
| 2 | 315 | 2.5 | 201,000 | 498 |
| 3 | 350 | 6.5 | 12,600 | 2 |
| 4 | 45 | 4.5 | 20,100 | 5 |
| 5 | 60 | 3.9 | 25,500 | 8 |
| 6 | 90 | 4.1 | 28,500 | 10 |
| 7 | 120 | 4.0 | 25,500 | 8 |
| 8 | 135 | 5.5 | 20,100 | 5 |
| 9 | 215 | 7.2 | 12,600 | 2 |
| 10 | 230 | 3.5 | 220,000 | 597 |
| 11 | 270 | 1.2 | 348,000 | 1495 |

For extra credit, students can use a protractor, compass and a 4-quadrant graph paper with axis marked in intervals of 1.0 Re, to plot each of the 11 points. A red and blue crayon can be used to code each point as a high-density region (red = 400 to 1500 electrons/cc) or a low-density region (blue = 1 to 10 electrons/cc).

The low-density regions are farther from Earth and represent the plasma, which fills Earth magnetic field. The high-density regions is closer to Earth and the satellite, and corresponds to the plasmasphere region of the upper atmosphere.

Name _____

Applications of the Pythagorean Theorem - Magnetism.

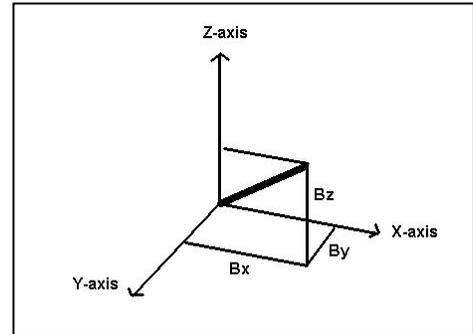
Unlike temperature, magnetism requires three numbers to define the strength of its field in space. Scientists call magnetism a **Vector** quantity because it is defined by both its magnitude at a point in space, and its direction at that point, given by the coordinate (X, Y, Z). The Pythagorean Theorem is used to calculate the magnitude (or total strength) of the magnetic field from the separate Bx, By and Bz quantities that make up its description as a field in 3-dimensional space. To find the Bx, By and Bz components of Earth's magnetic field (in units of nanoTeslas, nT) where you live, visit the International Geomagnetic Reference Field Model (Part 2 Form)

<http://nssdc.gsfc.nasa.gov/space/model/models/igrf.html>

Enter the year (2004) and the requested geographic latitude, longitude (in degrees, minutes and seconds – D M S entries in table) and elevation (Use 0.0 km for table). You can find the geographic coordinates for a specific location at

<http://geonames.usgs.gov>

Follow 'Query GNIS' to the input form. Select 'Civil' for a town name.



The Pythagorean Theorem in 3-dimensions is

$$D = \sqrt{x^2 + y^2 + z^2}$$

Use the Pythagorean Theorem to fill-in the last column of the table

| City | Longitude D M S | Latitude D M S | Bx (nT) | By (nT) | Bz (nT) | Total B (nT) |
|-------------|--------------------|-------------------|------------|------------|------------|-----------------|
| Chicago | 87 54 55 | 41 50 05 | 26600 | 1234 | 48620 | 55434 |
| Boston | 71 05 00 | 42 18 00 | 25251 | 2234 | 46676 | |
| Miami | 80 32 00 | 25 37 00 | 36274 | 0.2 | 28396 | |
| Hollywood | 118 20 00 | 34 01 00 | 32161 | -2684 | 39236 | |
| Bangor | 68 47 15 | 44 49 56 | 23437 | 2600 | 48244 | |
| Kansas City | 94 43 37 | 39 07 06 | 28846 | 365 | 46535 | |
| Sioux Falls | 96 43 48 | 43 32 48 | 25602 | 283 | 50988 | |
| Spokane | 117 22 00 | 47 37 00 | 22977 | -3263 | 53054 | |
| Provo | 103 52 06 | 43 10 02 | 26045 | -875 | 50767 | |
| Anchorage | 149 15 02 | 61 10 00 | 16377 | -3572 | 53739 | |
| Honolulu | 154 53 24 | 19 33 15 | 32644 | 1402 | 14594 | |
| Sedona | 111 47 35 | 34 50 38 | 31818 | -1978 | 41379 | |

Question 1 - What cities have the highest and lowest magnetic field (**B**) strengths?

Question 2 - What is the average **B** value of Earth's magnetic field for all locations?

Question 3 – Some adults think that Sedona Arizona has special 'powers'. How does the magnetism at this location compare to other locations in the table?

Question 4: Plot the **By** values on a map. What pattern do you see?

| City | Longitude D M S | Latitude D M S | Bx (nT) | By (nT) | Bz (nT) | Total B (nT) |
|-------------|--------------------|-------------------|------------|------------|------------|-----------------|
| Chicago | 87 54 55 | 41 50 05 | 26600 | 1234 | 48620 | 55434 |
| Boston | 71 05 00 | 42 18 00 | 25251 | 2234 | 46676 | 75116 |
| Miami | 80 32 00 | 25 37 00 | 36274 | 0.2 | 28396 | 65148 |
| Hollywood | 118 20 00 | 34 01 00 | 32161 | -2684 | 39236 | 71847 |
| Bangor | 68 47 15 | 44 49 56 | 23437 | 2600 | 48244 | 75941 |
| Kansas City | 94 43 37 | 39 07 06 | 28846 | 365 | 46535 | 77430 |
| Sioux Falls | 96 43 48 | 43 32 48 | 25602 | 283 | 50988 | 80688 |
| Spokane | 117 22 00 | 47 37 00 | 22977 | -3263 | 53054 | 81894 |
| Provo | 103 52 06 | 43 10 02 | 26045 | -875 | 50767 | 80701 |
| Anchorage | 149 15 02 | 61 10 00 | 16377 | -3572 | 53739 | 79609 |
| Honolulu | 154 53 24 | 19 33 15 | 32644 | 1402 | 14594 | 50607 |
| Sedona | 111 47 35 | 34 50 38 | 31818 | -1978 | 41379 | 73871 |

Question 1 - What cities have the highest and lowest magnetic field (**B**) strengths?

Answer: The city with the highest total magnetic field strength is Spokane, Washington (81894 nT). The city with the smallest total magnetic field strength is Honolulu, Hawaii (50607 nT)

Question 2 - What is the average **B** value of Earth's magnetic field for all locations?

Answer : $(55434 + 75116 + 65148 + 71847 + 75941 + 77430 + 80688 + 81894 + 80701 + 79609 + 50607 + 73871) / 12 = 868286/12 = \mathbf{72357\ nT}$

Remember to have the students give the answer in the correct physical units.

Question 3 – Some adults think that Sedona Arizona has special ‘powers’. How does the magnetism at this location compare to other locations in the table?

Answer: There are several things the student can note. 1) It has only the 8th strongest magnetic field out of 12 cities; 2) It has the third lowest Bz value (41379 nT); and 3) It has the fourth-lowest By value (-1978). None of these are as remarkable as what we find among the other large cities in this random sample.

Question 4: Plot the **By** values on a map. What pattern do you see?

Answer: The most obvious thing the students should notice is that:

- 1) The By magnetic values are always much smaller than for the Bx and Bz magnetic components. In fact they are typically only about 10% of the other two components;
- 2) The values to the east of longitude 100 to 105 degrees are positive. The values to the west are negative. **Note, the reason for this is that the longitude of the magnetic pole is 105 degrees, so this is the ‘axis of symmetry’ for these values.**

Magnetic forces and Particle Motion.

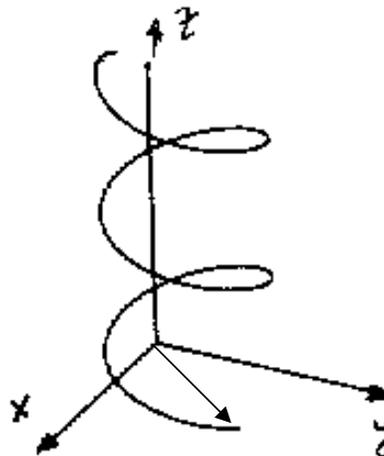
Magnetic forces are more complicated than gravity in several important ways. Unlike gravity, but similar to the ordinary Coulomb force between charged particles, magnetic forces depend on the degree to which a particle is charged. Also unlike gravity, magnetic forces possess a quality called 'polarity'. All magnets have both a north and a south 'pole'. Because of the property of polarity, the motion of charged particles in a magnetic field is more complicated than the motion under gravitational forces alone.

One common motion is for a charged particle to move in a spiral path along a line of magnetic force. As the particle moves along the field, it also executes a circular 'orbit' around the line of force, so its path resembles a helix. The spiral path can be thought of as a circular path with a radius, R , which moves at a constant speed along the line of force. Adding up the 'circular' and 'linear' motions of the particle gives you a spiral path like an unwound spring or 'Slinky' toy.

In this exercise, we will calculate the radius of such a spiral path and see how it depends on both the strength of the magnetic field, and the speed of the charged particle as it orbits the line of magnetic force. The formula for the radius of the spiral (shown by the arrow in the figure below) is given by:

$$q v B = \frac{m v^2}{R}$$

where q is the charge on the particle (in Coulombs), v is the speed of the particle as it orbits the line of force (in meters/s), B is the magnetic field strength (in Teslas), m is the mass of the particle (in kilograms), and R is the radius of the particle's orbit (in meters).



Question 1 – What is the relationship for R after solving and simplifying this equation?

Question 2 – An electron with a charge $q = 1.6 \times 10^{-19}$ Coulombs and a mass $m = 9.1 \times 10^{-31}$ kilograms is traveling at $v = 1.0 \times 10^9$ meters/sec in a magnetic field with a strength $B = 0.00005$ Teslas. What is the radius of its spiral orbit in meters?

Question 3 - If an oxygen ion has twice the electron's charge, and 29400 times an electron's mass, what will its spiral radius be for the same values of B and v in Question 1?

Question 1 - What is the relationship for R after solving and simplifying this equation?

Answer: After a little algebra:

$$q v B = \frac{m v^2}{R} \quad \text{becomes}$$

$$R = \frac{m v}{q B}$$

Question 2 – An electron with a charge $q = 1.6 \times 10^{-19}$ Coulombs and a mass $m = 9.1 \times 10^{-31}$ kilograms is traveling at $V = 1.0 \times 10^9$ meters/sec in a magnetic field with a strength $B = 0.00005$ Tesslas. What is the radius of its spiral orbit in meters?

Answer: From the equation that we just solved for R in Question 1,

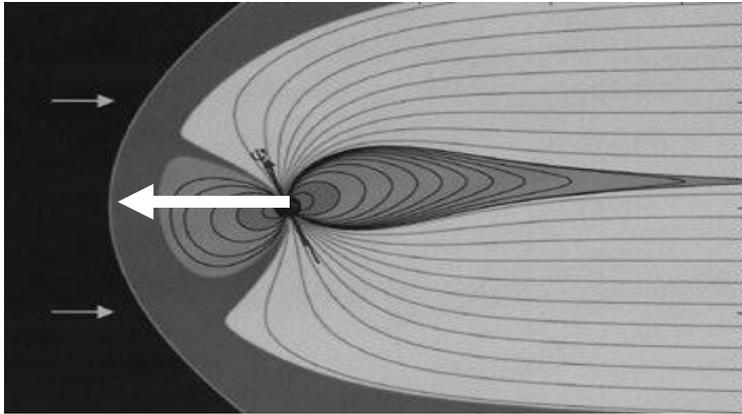
$$R = (9.1 \times 10^{-31}) \times (1.0 \times 10^9) / (1.6 \times 10^{-19} \times 0.00005)$$

$$R = (9.1 \times 1.0 / (1.6 \times 5)) \times 10^{(-31 + 9 + 19 + 5)}$$

$$R = 113 \text{ meters.}$$

Question 3 - If an oxygen ion has twice the electrons charge, and 29400 times an electron's mass, what will its spiral radius be for the same values of B and V in Question 1?

Answer: The formula says that if you double the charge, the radius is decreased by $\frac{1}{2}$. If you increase the mass by 29400 times, then the radius will also increase by the same amount. So, the net change in R is $(29,400/2) = 14700$ times the electron's radius or $14700 \times 113 \text{ meters} = 1.66 \text{ million meters}$ or 1,660 kilometers. Students can solve it this way, or simply substitute into the equation for R, $B = 0.00005$, $V = 1.0 \times 10^9$, $q = 2 \times (1.6 \times 10^{-19})$, $m = 29400 \times 9.1 \times 10^{-31}$



When the solar wind flows past Earth, it pushes on Earth's magnetic field and compresses it. There is a point in space called the magnetopause where the pressure of the solar wind balances the outward pressure of Earth's magnetic field. The distance from the Earth, R , (white arrow in drawing) where these two pressures are balanced is given by the equation:

$$R^6 = \frac{0.72}{8\pi DV^2}$$

In this equation, D is the density in grams per cubic centimeter (cc) of the gas (solar wind, etc) that collides with Earth's magnetic field, and V is the speed of this gas in centimeters per second. Let's do an example to see how this equation works!

The solar wind has a typical speed of 450 km/s or equivalently $V = 4.5 \times 10^7$ cm/s. To find the density of the solar wind in grams/cc we have to do a two-step calculation. The wind usually has a particle density of about 5 particles/cc, and since these particles are typically protons (each with a mass of 1.6×10^{-24} gm) the density is then $5 \times (1.6 \times 10^{-24}$ gm)/cc so that $D = 1.28 \times 10^{-23}$ gm/cc.

We substitute D and V into the equation and get $R^6 = 1105242.6$. so that $R = (1105242.6)^{1/6}$. To solve this, we use a calculator with a key labeled Y^x . First type '1105242.6' and hit the 'Enter' key. Then type '0.1666' (which equals 1/6) and press the Y^x key. In this case the answer will be '10.16' and it represents the value of R in multiples of the radius of Earth (6378 kilometers). Scientists simplify the mathematical calculation by using the radius of Earth as their unit of distance, but if you want to convert 10.16 Earth radii to kilometers, just multiply it by '6378 km' which is the radius of Earth to get 64,800 kilometers. That is the distance from the center of Earth to the magnetopause where the magnetic pressure is equal to the solar wind pressure for the selected speed and density. These will change significantly during a 'solar storm'.

Now lets apply this example to finding the magnetopause distance for some of the storms that have encountered Earth in the last five years. Complete the table below, rounding the answer to three significant figures:

| Storm | Date | Day Of Year | Density (particle/cc) | Speed (km/s) | R (km) |
|-------|------------|-------------|-----------------------|--------------|--------|
| 1 | 11/20/2003 | 324 | 49.1 | 630 | |
| 2 | 10/29/2003 | 302 | 10.6 | 2125 | |
| 3 | 11/06/2001 | 310 | 15.5 | 670 | |
| 4 | 3/31/2001 | 90 | 70.6 | 783 | |
| 5 | 7/15/2000 | 197 | 4.5 | 958 | |

Question: The fastest speed for a solar storm 'cloud' is 1500 km/s. What must the density be in order that the magnetopause is pushed into the orbits of the geosynchronous communication satellites at 6.6 Re?

The information about these storms and other events can be obtained from the NASA ACE satellite by selecting data for H* density and V_x(GSE)

http://www.srl.caltech.edu/ACE/ASC/level2/lvl2DATA_MAG-SWEPAM.html

| Storm | Date | Day Of Year | Density (particle/cc) | Speed (km/s) | R (km) |
|-------|------------|-------------|-----------------------|--------------|--------|
| 1 | 11/20/2003 | 324 | 49.1 | 630 | 42,700 |
| 2 | 10/29/2003 | 302 | 10.6 | 2125 | 37,000 |
| 3 | 11/06/2001 | 310 | 15.5 | 670 | 51,000 |
| 4 | 3/31/2001 | 90 | 70.6 | 783 | 37,600 |
| 5 | 7/15/2000 | 197 | 4.5 | 958 | 54,800 |

Question: The fastest speed for a solar storm 'cloud' is 3000 km/s. What must the density be in order that the magnetopause is pushed into the orbits of the geosynchronous communication satellites at 6.6 Re (42,000 km)?

Answer: Solve the equation for D to get:

$$D = \frac{0.72}{8 \pi R^6 V^2}$$

For 1500 km/s $V = 1.5 \times 10^8$ cm/s, and for $R = 6.6$, we have

$$D = 0.72 / (8 \times 3.14 \times 6.6^6 \times (1.5 \times 10^8)^2) = 1.52 \times 10^{-23} \text{ gm/cc}$$

Since a proton has a mass of 1.6×10^{-24} grams, this value for the density, D, is equal to $(1.52 \times 10^{-23} / 1.6 \times 10^{-24}) = 9.5$ protons/cc.

For Extra Credit, have students compute the density if the solar storm pushed the magnetopause to the orbit of the Space Station (about $R = 1.01$ RE).

Answer: $D = 3 \times 10^{-19}$ gm/cc or 187,000 protons/cc. A storm with this density has never been detected, and would be catastrophic!

Kinetic Energy and Voltage.

When matter moves, it possesses a quantity of energy called Kinetic Energy. This energy can be described by a simple mathematical formula. When matter that carries a charge moves in an electric field, it also carries kinetic energy. By comparing the two mathematical descriptions of kinetic energy, we can relate how the speed of a particle, V , changes as its mass, m , charge, q , or the electrical voltage, E , it moves in, is changed. Scientists often measure a charged particle's kinetic energy in terms of its voltage. In this exercise, we will look at the energies of various types of charged particle systems and determine the average speed of the particle. The formula that relates the kinetic energy of a particle to its voltage is given below. The left side is the definition for kinetic energy based on its charge and the voltage, E . The right side is the definition of kinetic energy based on the particles mass and speed.

$$qE = \frac{1}{2} m V^2$$

Question 1 – What is the formula for the speed of the particle, V , after solving the equation for V , and simplifying?

Question 2 – An electron with a charge $q = 1.6 \times 10^{-19}$ Coulombs and a mass $m = 9.1 \times 10^{-31}$ kilograms and has an energy $E = 1000$ Volts. What is the speed of the particle in meters per second?

Question 3 - If an oxygen ion has twice the charge of an electron, and 29400 times an electron's mass, what will its speed be for the same amount of energy $E = 1,000$ Volts?

Question 1 - What is the relationship for **V** after solving and simplifying this equation?

Answer: After a little algebra:

$$qE = \frac{1}{2} m V^2 \quad \text{becomes}$$

$$V = \sqrt{\frac{2qE}{m}}$$

Question 2 – An electron with a charge $q = 1.6 \times 10^{-19}$ Coulombs and a mass $m = 9.1 \times 10^{-31}$ kilograms and has an energy $E = 1000$ Volts. What is the speed of the particle in meters per second?

Answer:

$$V^2 = (2 \times 1.6 \times 10^{-19} \times 1000) / (9.1 \times 10^{-31})$$

$$V^2 = (2 \times 1.6 / 9.1) \times 10^{(-19 + 3 + 31)}$$

$$V^2 = 3.5 \times 10^{14}$$

$$V = 1.9 \times 10^7 \text{ meters/sec or } 19,000 \text{ kilometers/sec.}$$

Question 3 - If an oxygen ion has twice the charge of an electron, and 29400 times an electron's mass, what will its speed for the same amount of energy $E = 1,000$ Volts?

Answer: Because the mass and charge appear under the square root sign, the oxygen atom will travel at a speed $(2/29400)^{1/2}$ or 0.0082 times slower than the electron. The speed will be $V = 0.0082 \times 1.9 \times 10^7 = 139$ kilometers per second. Students can verify this by direct substitution of the new q and m into the equation, and converting to kilometers/sec.

Useful Internet Resources

The human and technological impacts of solar storms and space weather:

<http://www.solarstorms.org>

Newspaper accounts of aurora and technology impacts from 1800-2001:

<http://www.solarstorms.org/SRefHistory.html>

Space weather and satellite failures

<http://www.solarstorms.org/Ssatellites.html>

NOAA space weather forecasting center

<http://www.noaa.sec.gov/SWN>

Space weather summaries and daily updates:

<http://www.spaceweather.com>

NASA Student Observation Network –Tracking a Solar Storm

<http://son.nasa.gov/tass/index.htm>

Archive of NASA TV programs about space weather for grades 6-10

<http://www.solarstorms.org/STV.html>

Movies and animations about space weather

<http://www.solarstorms.org/SMovies.html>

Frequently Asked Questions about space weather

<http://www.solarstorms.org/SFAQs.html>

Additional classroom activities

<http://image.gsfc.nasa.gov/poetry/activities.html>

Exploring Space Science Mathematics pre-algebra problem book

<http://image.gsfc.nasa.gov/MathDocs/spacemath.html>

Exploring Earth's Magnetic Field primer

<http://image.gsfc.nasa.gov/poetry/magnetism/magnetism.html>

IMAGE, Student's Guide to Sun-Earth Science topics

<http://image.gsfc.nasa.gov/poetry/educator/students.html>

The IMAGE, Soda Bottle Magnetometer

<http://image.gsfc.nasa.gov/poetry/workbook/magnet.html>

The Mysterious Van Allen Radiation Belts

<http://radbelts.gsfc.nasa.gov/outreach/outreach.html>



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