



The LRO satellite recently imaged the Apollo 11 landing area on the surface of the moon. The above (172 pixels wide x 171 pixels high) image shows this area and is 172 meters wide.

**Problem 1** - Determine the scale of the image in meters per millimeter and meters per pixel? What is the diameter, in meters, of A) the largest crater? B) the smallest crater?

**Problem 2** - The shadow near the center of the picture was cast by the Lunar Landing Module which is about 3.5 meters tall. Using A) trigonometry, or a B) scaled drawing and a protractor, what was the sun angle at the time of the photograph?

**Problem 3** - Are there any individual boulders larger than 1 meter across in this area?

**Problem 1** - Determine the scale of the image in meters per millimeter and meters per pixel? What is the diameter, in meters, of A) the largest crater? B) the smallest crater?

Answer: The image is 153 millimeters wide, which corresponds to 172 meters, so the scale is **1.1 meters per millimeter**, and the image is 172 pixels wide so the resolution is 172 pixels/153 meters = **1.1 meters/pixel**.

The largest crater is about 25mm x 30 mm in size, which corresponds to 25mm x 1.1 meters/mm = 28 meters wide, and 30 mm x 1.1 = 33 meters long, for an **average size of about 30 meters across**. B) The smallest discernable features are about 1 to 2 mm wide, which corresponds to an actual size of about 1-2 pixels or 1 to 2 meters. Note, there can be no actual details smaller than the pixel resolution of the image (1.1 meters).

**Problem 2** - The shadow near the center of the picture was cast by the Lunar Landing Module which is about 3.5 meters tall. Using A) trigonometry, or a B) scaled drawing and a protractor, what was the sun angle at the time of the photograph?

Answer: The length of the shadow from the base of the lander is about 23 millimeters or in actual length, 23 x 1.1 = 25 meters. This makes a right triangle, ABC, with a base length AB= 25 meters and an altitude of AC=3.5 meters and a hypotenuse located along BC, with the right-angle defined as ABC.

Method 1: From trigonometry,  $\tan(\theta) = 3.5 \text{ meters} / 25 \text{ meters} = 0.14$  so the angle whose tangent is 0.14 is  **$\theta = 8.0 \text{ degrees}$** .

Method 2: A scaled drawing is shown below, and a protractor may be used to measure the angle directly from the diagram.

**Problem 3** - Are there any individual boulders larger than 1 meter across in this area?

Answer: No, because they would have shadows about 7 meters long (1/4 the Apollo 11 module) and there are no such shadows in the image, other than the Apollo-11 Landing Module itself. This area of the moon seems to be boulder-free at a resolution of 1 meter, which is why it was selected by Apollo-11 astronauts for a landing site.

