



Rocket engines work by throwing matter out the back end of a rocket as fast as they can. Usually this matter is in the form of gas. This causes the rocket to move forward in the opposite direction from the ejected matter, thanks to Newton's Third Law of Motion which says that *'For every Action, there is an equal and opposite Reaction'*.

To lift tons of cargo into space, rocket engines have to be very powerful. Engineers usually compare different engines by their thrust and by their specific impulse. This makes it easy to decide which kind of engine to use to put different payloads into space in the most efficient and low-cost way possible.

Problem 1 – Specific Impulse $I_{sp} = V/g$ is the ratio of the exhaust speed of the engine (V) divided by the acceleration of gravity at Earth's surface (g), where g is 9.8 meters/sec² and V is measured in meters/sec. The J-2X rocket engine has an $I_{sp}=421$ seconds. How fast are the exhaust gases leaving the bottom of the engine in A) kilometers/sec? B) feet per second? C) miles per hour? (1 kilometer = 3280 feet; 1 mile = 5280 feet)

Problem 2 – Thrust is a measure of the force that the rocket can produce to move an object against the pull of gravity. It is measured in Newtons and is defined by $\text{Thrust} = F \times V$ where F is the rate of flow of fuel in kilograms/sec and V is the exhaust speed of the combusted gases. The new J-2X rocket engines being designed and tested by NASA have an $I_{sp}=421$ seconds and a thrust of $T = 1,310,000$ Newtons. At what rate is mass leaving the rocket engine in A) kilograms/second? B) pounds/second? (1 kilogram = 2.2 pounds).

Problem 3 – Ion rocket engines: Instead of chemical rockets using liquid fuels, the Dawn spacecraft has an ion rocket with $I_{sp}=3,100$ seconds. If the same ion technology was used to design a replacement for the liquid-fueled J-2X engine, what must be the fuel flow rate, F , in order to produce the same thrust as the J-2X engine?

Problem 4 – Rocket Design: What would the I_{sp} and thrust be for an engine that had $V = 10,000$ meters/sec and $F = 500$ kg/sec?

<http://www.grg.northwestern.edu/projects/vss/docs/propulsion/3-how-you-calculate-specific-impulse.html>

Problem 1 – Specific Impulse $I_{sp} = V/g$ is the ratio of the exhaust speed of the engine (V) divided by the acceleration of gravity at Earth's surface (g), where g is 9.8 meters/sec^2 and V is measured in meters/sec. The J-2X rocket engine has an $I_{sp}=421$ seconds. How fast are the exhaust gases leaving the bottom of the engine in A) kilometers/sec? B) feet per second? C) miles per hour? (1 meter = 3.280 feet; 1 mile = 5280 feet)

Answer: A) $I_{sp}=421$ seconds and $g = 9.8 \text{ m/sec}^2$ so $V = I_{sp} \times g$ and
 $V = \mathbf{4,126 \text{ meters/second}}$.

B) 1 meter = 3.28 feet and so $V = 4126 \text{ m/s}$ ($3.28 \text{ feet/1 meter}$) so
 $V = \mathbf{13,533 \text{ feet/sec}}$.

C) 1 mile = 5280 feet so $V = 13,533/5280 = 2.56 \text{ miles/sec}$ and for 3600 seconds in 1 hour, we have $V = \mathbf{9,216 \text{ miles/hour}}$.

Problem 2 – Thrust is a measure of the force that the rocket can produce to move an object against the pull of gravity. It is measured in Newtons and is defined by $\text{Thrust} = F \times V$ where F is the rate of flow of fuel in kilograms/sec and V is the exhaust speed of the combusted gases. The new J-2X rocket engines being designed and tested by NASA have an $I_{sp}=421$ seconds and a thrust of $T = 1,310,000$ Newtons. At what rate is mass leaving the rocket engine in A) kilograms/second? B) pounds/second? (1 kilogram = 2.2 pounds).

Answer: A) $I_{sp} = V/g$ so $V = 421 \times 9.8 \text{ m/sec}^2 = 4,126 \text{ meters/sec}$, then $T = F \times V$ and $F = T/V$ so $F = 1,310,000/4126 = \mathbf{317 \text{ kg/second}}$. B) $317.5 \text{ kg/sec} \times (2.2 \text{ pounds/1kg}) = \mathbf{698 \text{ pounds/second}}$.

Problem 3 – Ion rocket engines: Instead of chemical rockets using liquid fuels, the Dawn spacecraft has an ion rocket with $I_{sp}=3,100$ seconds. If the same ion technology was used to design a replacement for the liquid-fueled J-2X engine, what must be the fuel flow rate, F , in order to produce the same thrust as the J-2X engine?

Answer: $I_{sp} = 3100 \text{ sec}$ so $V = 3100 \text{ sec}/9.8 \text{ m/sec}^2 = 316 \text{ m/sec}$. $T = F \times V$ and $T = 1,310,000$ Newtons and so $F = 1,310,000/316 = \mathbf{4,145 \text{ kg/sec}}$.

Problem 4 – Rocket Design: What would the I_{sp} and thrust be for an engine that had $V = 10,000$ meters/sec and $F = 5000$ kg/sec?

Answer: $I_{sp} = 10,000/9.8 = \mathbf{1020 \text{ sec}}$, and $T = 5000 \times 1020 = \mathbf{5,100,000 \text{ Newtons}}$